



国家自然科学基金委员会  
National Natural Science Foundation of China



日本学術振興会  
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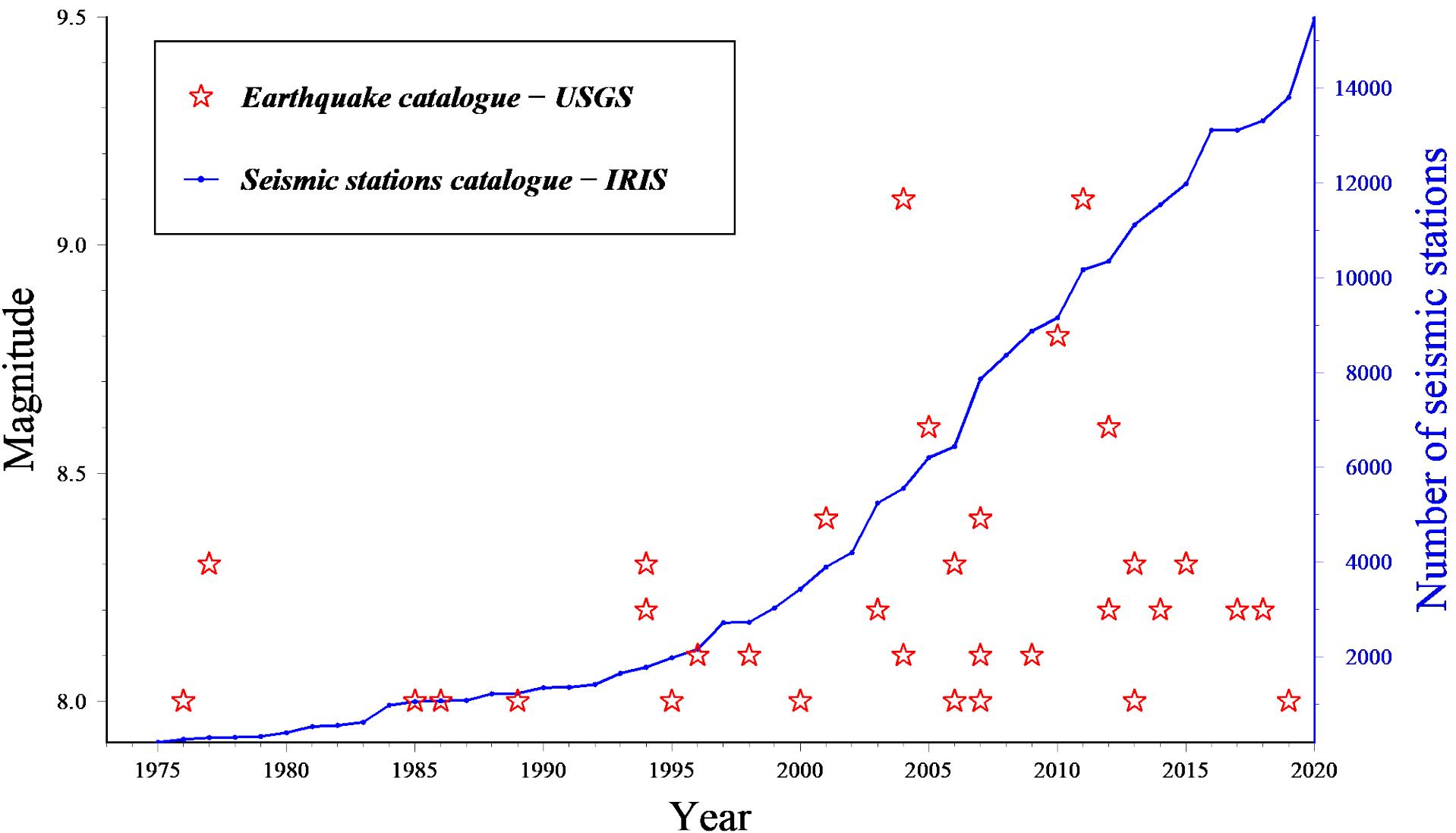
# Seismic Arrays: Insight into Source Characteristics and Disaster Mitigation

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Kyoto University  
The University of Tokyo

Online, 9 December, 2021

# Booming of seismic observations

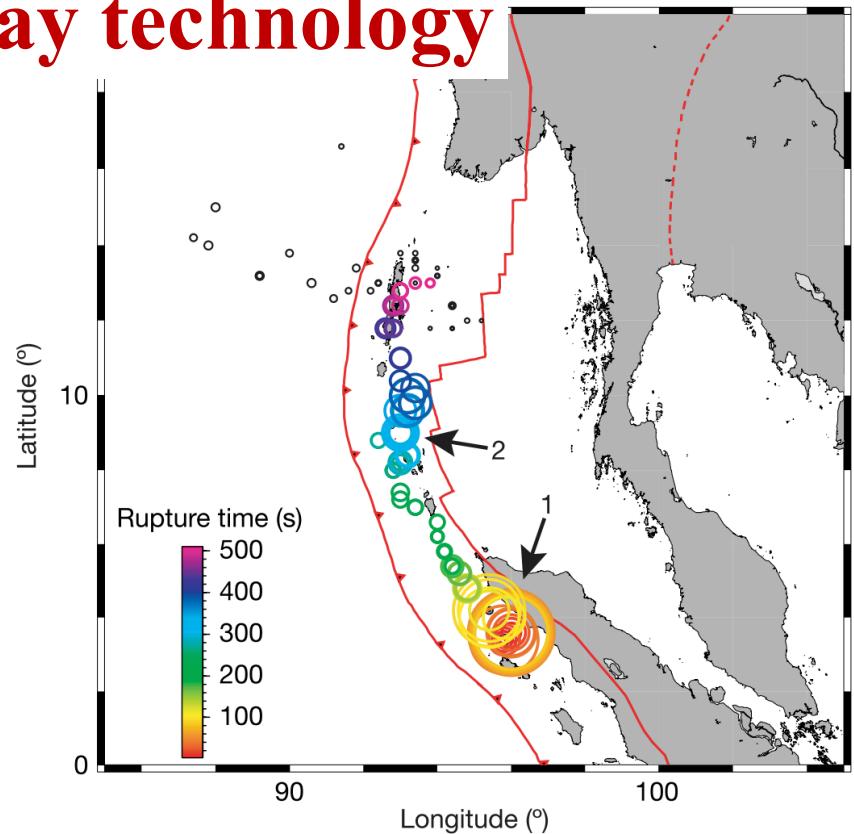


# Imaging source process of large earthquakes using seismic data recorded at dense arrays

**Big data + Array technology**



(Ishii et al., 2005, Nature)

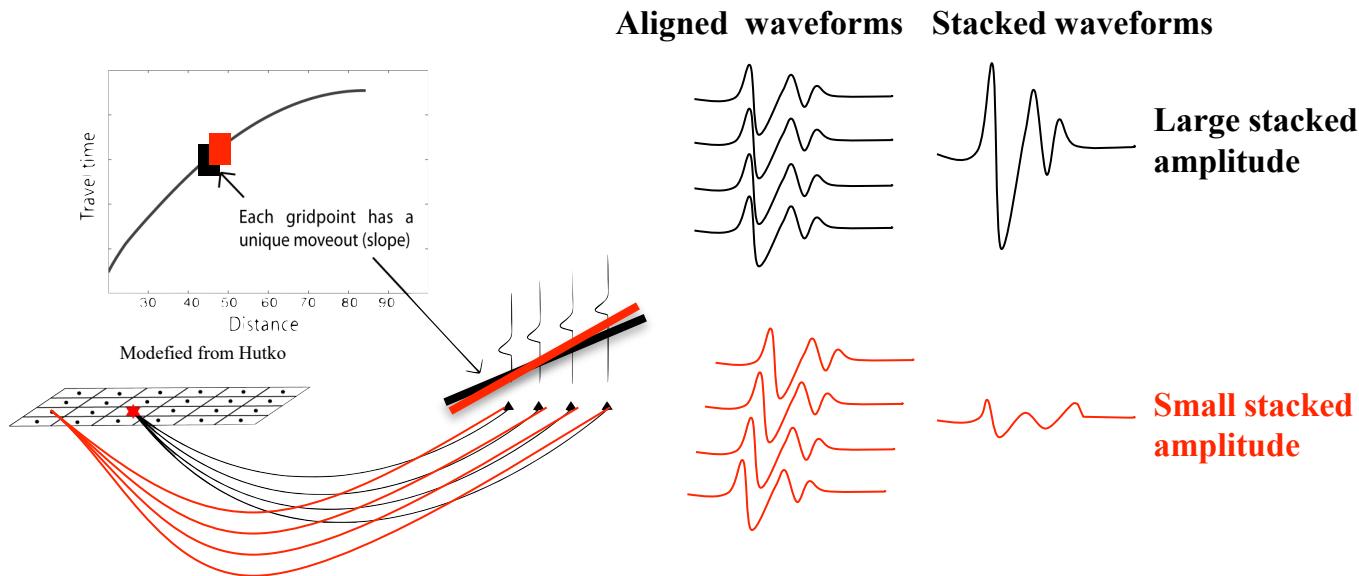


**Figure 3 | Rupture trace of the Sumatra earthquake.** Maxima of energy maps are shown in their spatiotemporal development by coloured circles. The width of the circles scales linearly with seismic energy; colour coding is proportional to the time since rupture initiation in the source region. Major tectonic lines are shown in red. Numbers 1 and 2 indicate the position of two major seismic energy releases.

(Kruger and Ohrnberger, 2005, Nature)

# Back-projection

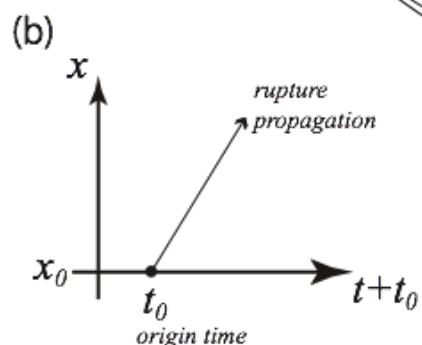
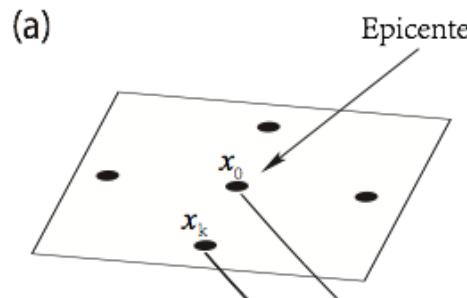
- Search a grid of points to determine the best location for the source of seismic radiation in each designated time window of interested waves.



# Two Back-projections

## Standard back-projection

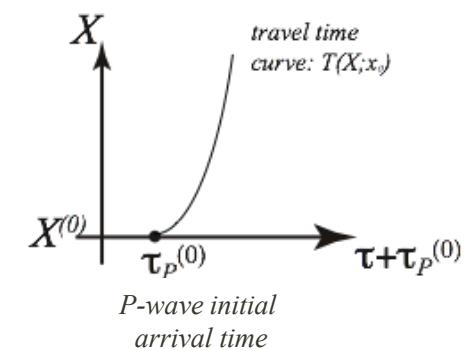
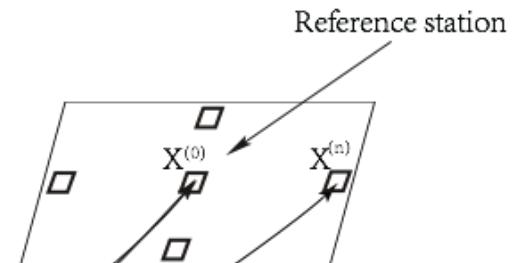
Ishii et al., 2005, Nature



## Sliding window beampacking

(Beamforming)

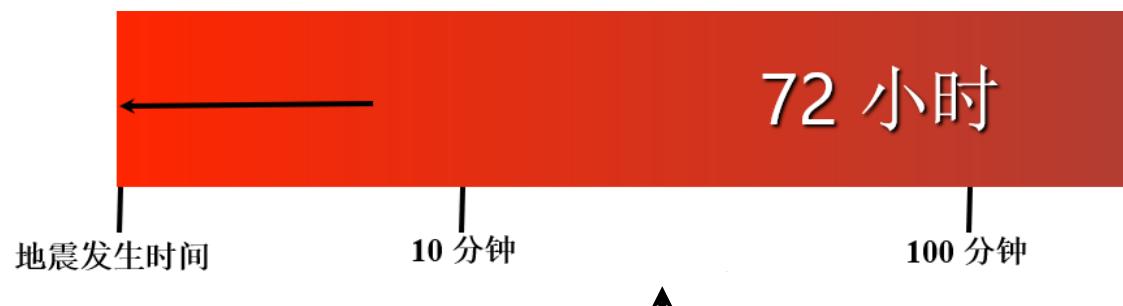
Krüger and Ohrnberger, 2005, Nature



(Wang et al., 2016)

# Determining magnitude of large earthquakes

- Rapidly and accurately determining magnitude of large earthquakes remains challenges



美国地调局  
(USGS)      5-13 min      32 min  
                         $M_{Wp}$  7.9       $M_W$  8.9

日本气象厅  
(JMA)      4-24min  $M_{Wp}$  7.9  
                        Tsunami warning  
                        base on M7.9

Hayes et al., 2011, SRL

The 2011 M9 Tohoku,  
Japan earthquake



Huge unexpected tsunami reached  
the Japan coast 25min after the  
earthquake

# The importance of accurate magnitude for tsunami warning

(With Tung-Cheng Ho, Kyoto University)

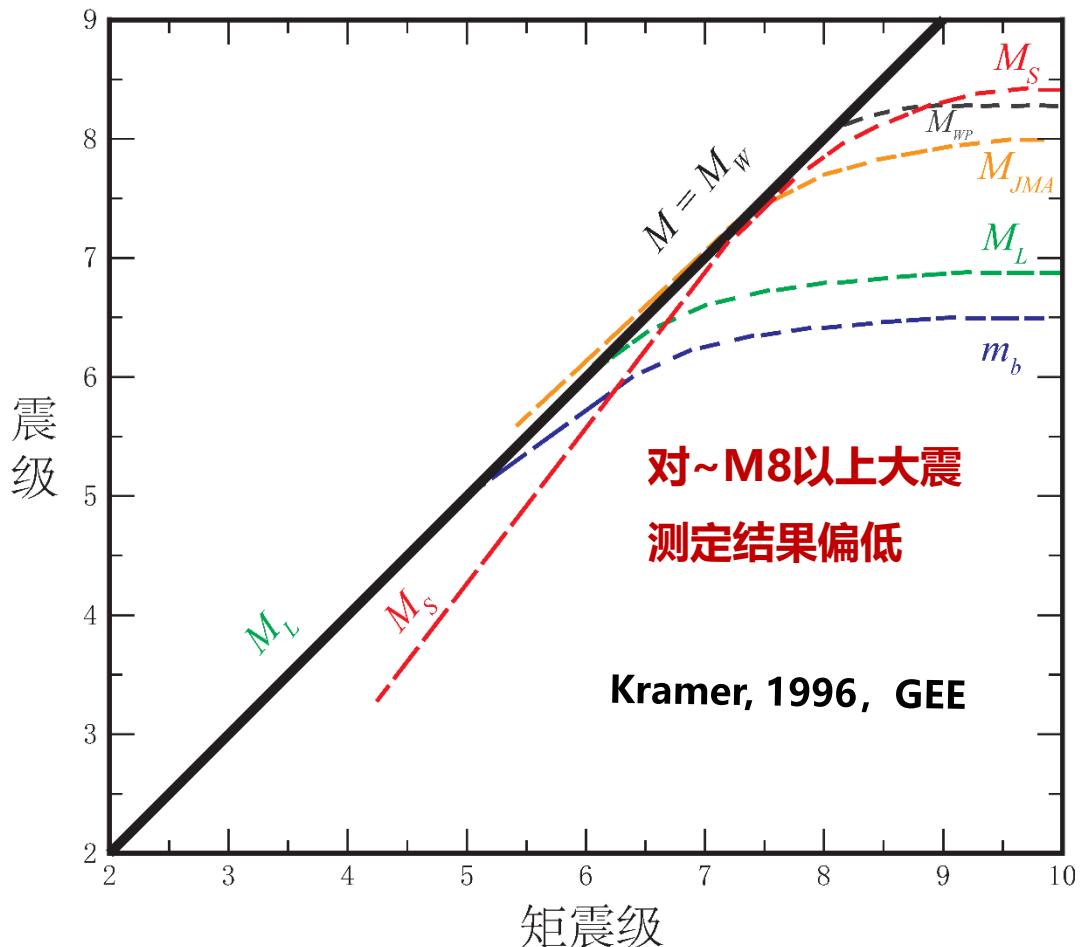
**M7.9**

**M9.1**



# Limitations of conventional methods

- $M_L$ 、 $M_S$ 、 $M_{WP}$ 、 $M_{JMA}$  Saturate for large earthquakes



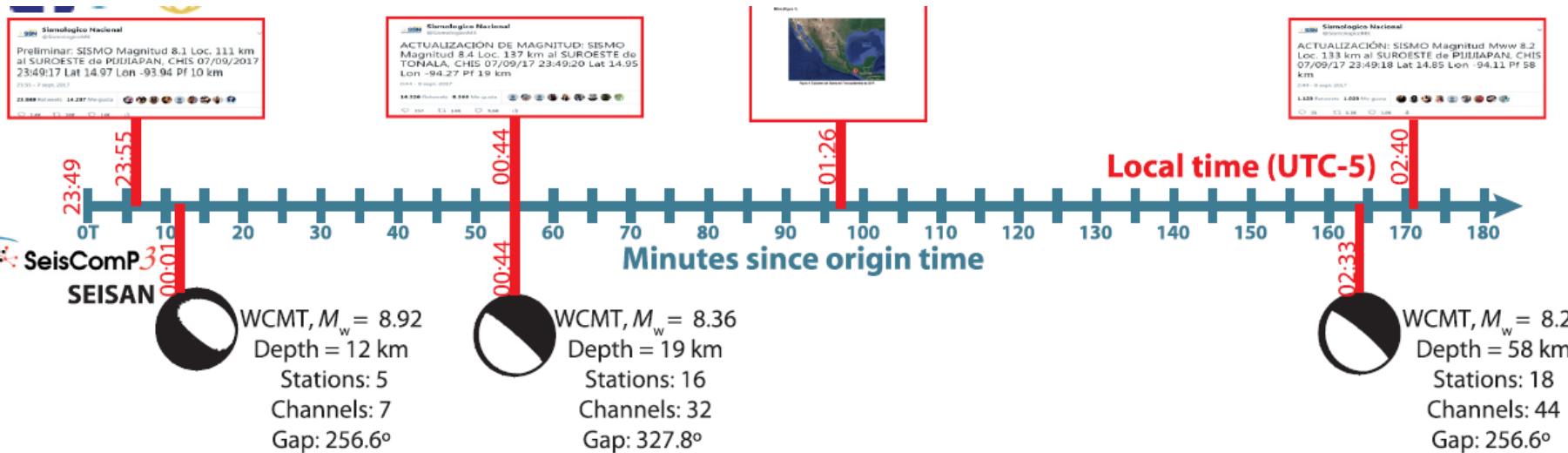
- $M_L$ 、 $M_S$ 、 $M_{WP}$ 、 $M_{JMA}$  saturate
- Ignoring source durations
- $M_{WW}$  is obtained from inversion of W-phase data, which may encounter instable results with limited data in the early phase after earthquakes.

# Sepetember 8, 2018 Mw 8.2 Mexico earthquake

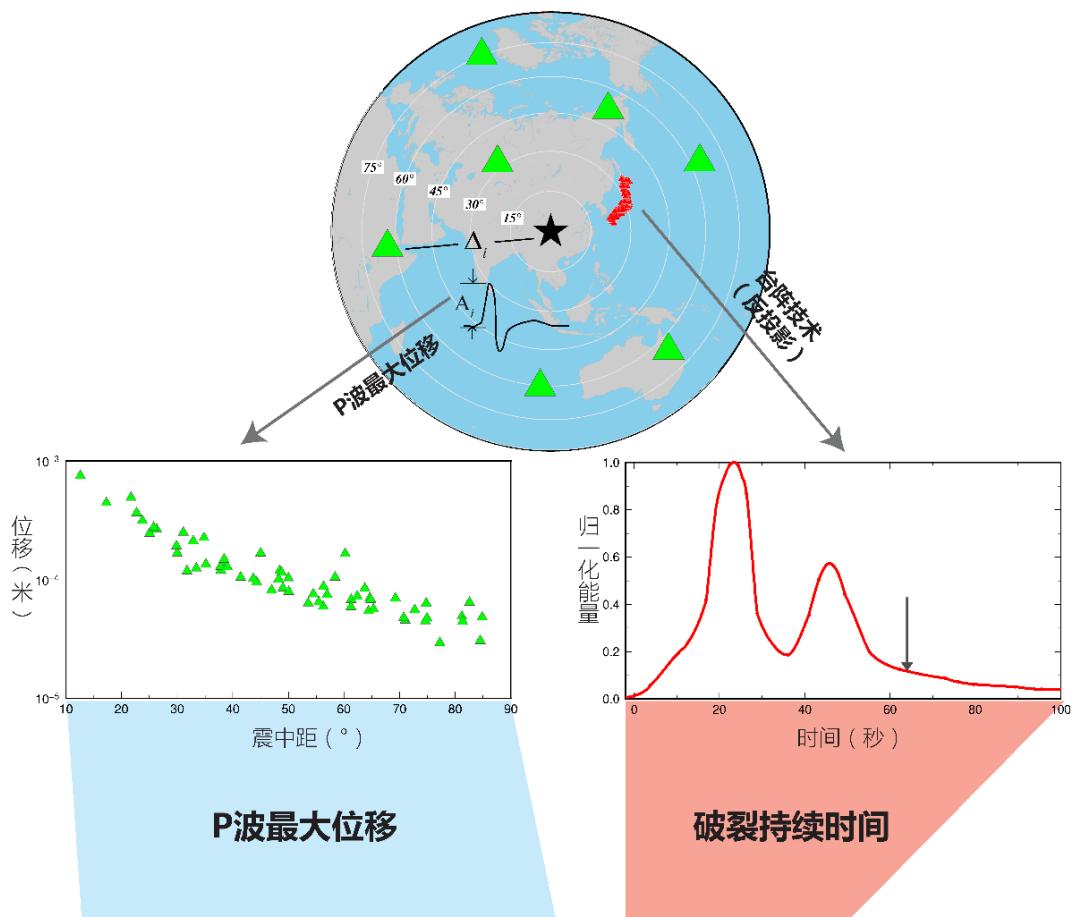
~10 min  
Mww 8.92

~1 h  
Mww 8.36

~2 h  
Mww 8.26



# A new magnitude scale (Hara, 2007; 2011; Wang et al., 2017)



GSN  
+  
Regional seismic array

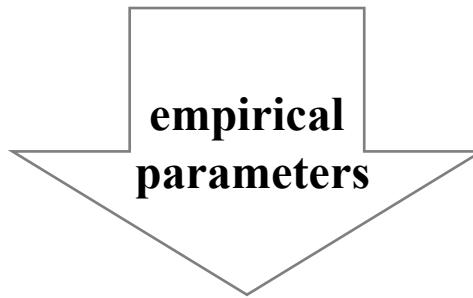
- P-wave displacements + source duration
- Rapid and straightforward

$$M = \alpha \log A + \beta \log \Delta + \gamma \log t + \delta$$

Wang et al., 2017

# $M_{dt}$ : P-wave Maximum Displacement & Source Duration

$$M = \alpha \log A + \beta \log \Delta + \gamma \log t + \delta$$



*10-40 ° , 40-85 ° , 10-85 °*

$\alpha$ : **0.79**  $\pm$  0.03,    0.53,    0.51,    0.55

$\beta$ : **0.83**  $\pm$  0.05,    0.44,    0.01,    0.67

$\gamma$ : **0.69**  $\pm$  0.03,    1.01,    1.05,    1.01

$\delta$ : **6.47**  $\pm$  0.17,    6.23,    7.89,    5.55

(Hara, 2007, 2008, 2011)

(Wang et al., 2017; Song et al., 2019; Yao et al., 2019)

# Far-field Displacement → Seismic Moment

- $A^{FP}$  and  $A^{FS}$ : P- and S-wave radiation pattern correction terms
  - $\rho$ : rock density
  - $\alpha$  and  $\beta$ : P- and S-wave velocity
  - $r$ : source-receiver distance
  - $M_0$ : moment rate function.

$$\mathbf{u}^P = \frac{1}{4\pi\rho\alpha^3} \mathbf{A}^{FP} \frac{1}{r} \dot{M}_0 \left( t - \frac{r}{\alpha} \right)$$

$$\dot{M}_0 = 4\pi\rho\alpha^3 r \frac{1}{\mathbf{A}^{FP}} \mathbf{u}^P$$

# Far-field Displacement → Seismic Moment

$$\dot{M}_0(\max) = 4\pi\rho\alpha^3 \cdot r \cdot u_{(\max)}^p$$

$(\dot{M}_0)^{\max}$



*Duration*

$$M_0 = (4\pi p a^3 \cdot R \cdot A) \cdot D$$

*Duration*

$$M_0 = (4\pi p a^3 \cdot R \cdot A) \cdot D \cdot 1/2$$

In Mwp method:

■  $\rho$ , rock density: 3.4E+03 kg/m<sup>3</sup>

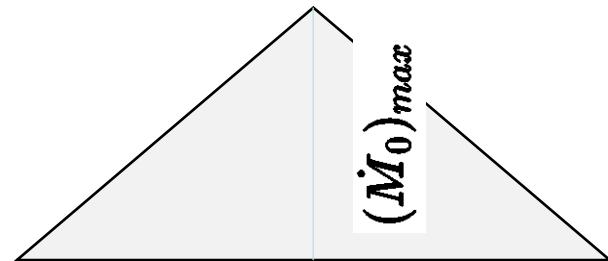
■  $\alpha$ , P velocity: 7.9 km/s

$$m * s * km * 4 * 3.14 * (3.4 * 10^3 \text{ kg/m}^3) * (7.9 \text{ km/s})^3$$

$$4 * 3.14 * 3.4 * 10^3 * 7.9^3 * (\text{kg} * \text{m/s}^2) * (\text{km}^4/\text{m}^3)$$

$$4 * 3.14 * 3.4 * 10^3 * 7.9^3 * 10^{12} Nm$$

$$2.1 * 10^{19} Nm$$



# Far-field Displacement → Seismic Moment

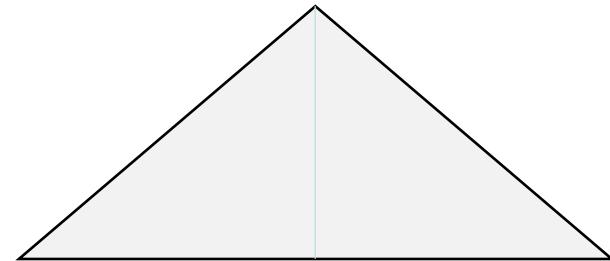
$(\dot{M}_0)_{max}$



*Duration*

$$M_0 = (4\pi p a^3 \cdot R \cdot A) \cdot D$$

$(\dot{M}_0)_{max}$



*Duration*

$$M_0 = (4\pi p a^3 \cdot R \cdot A) \cdot D \cdot 1/2$$

$$M = \frac{2}{3} [\log(M_0) - 9.1]$$

$$M_{dt} = \frac{2}{3} [\log(4\pi p a^3 \cdot R \cdot A \cdot D) - 9.1]$$

$$M_{dt} = \frac{2}{3} [\log(4\pi p a^3 \cdot R \cdot A \cdot D \cdot 1/2) - 9.1]$$

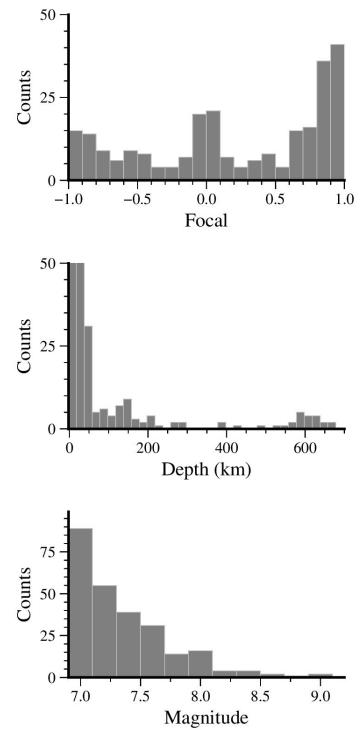
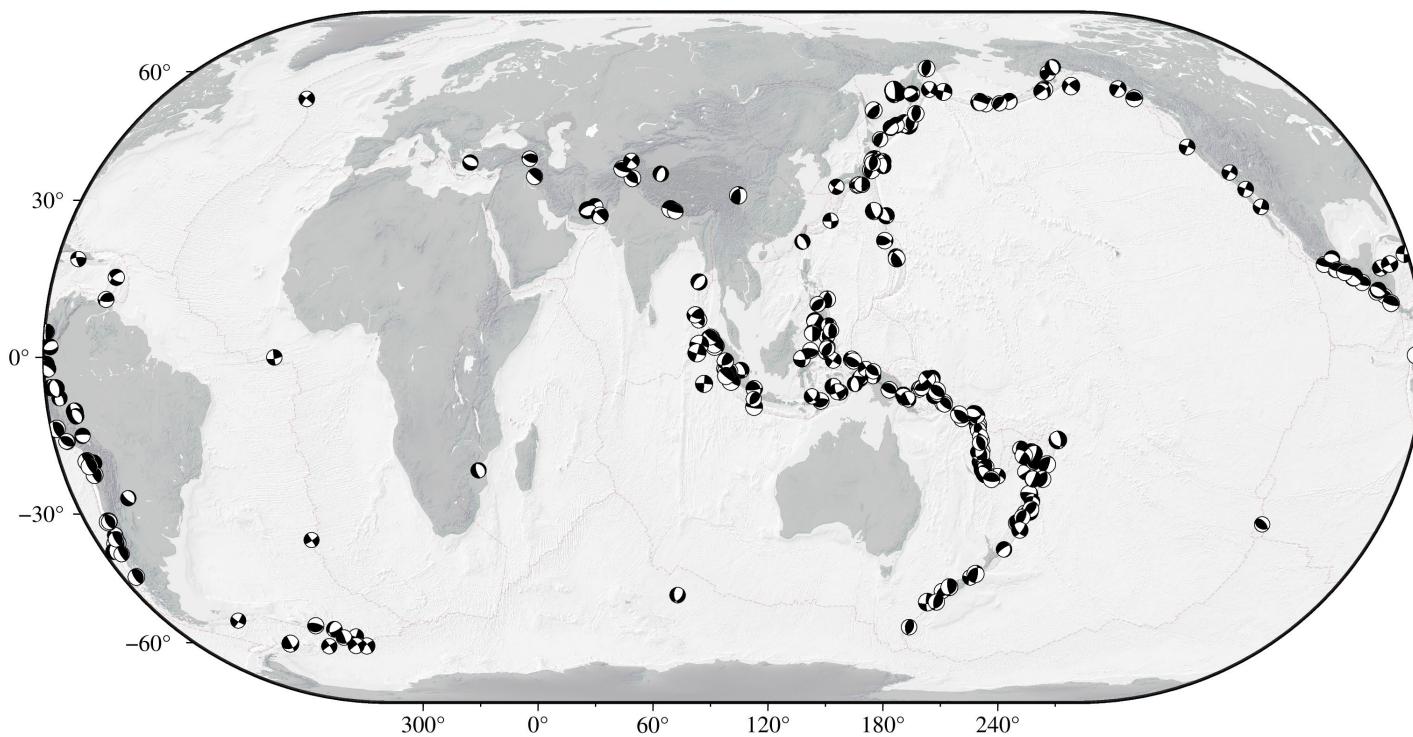
$$M_{dt} = 0.67 * \log A + 0.67 * \log R + 0.67 * \log D + \delta$$

$\delta=6.81$

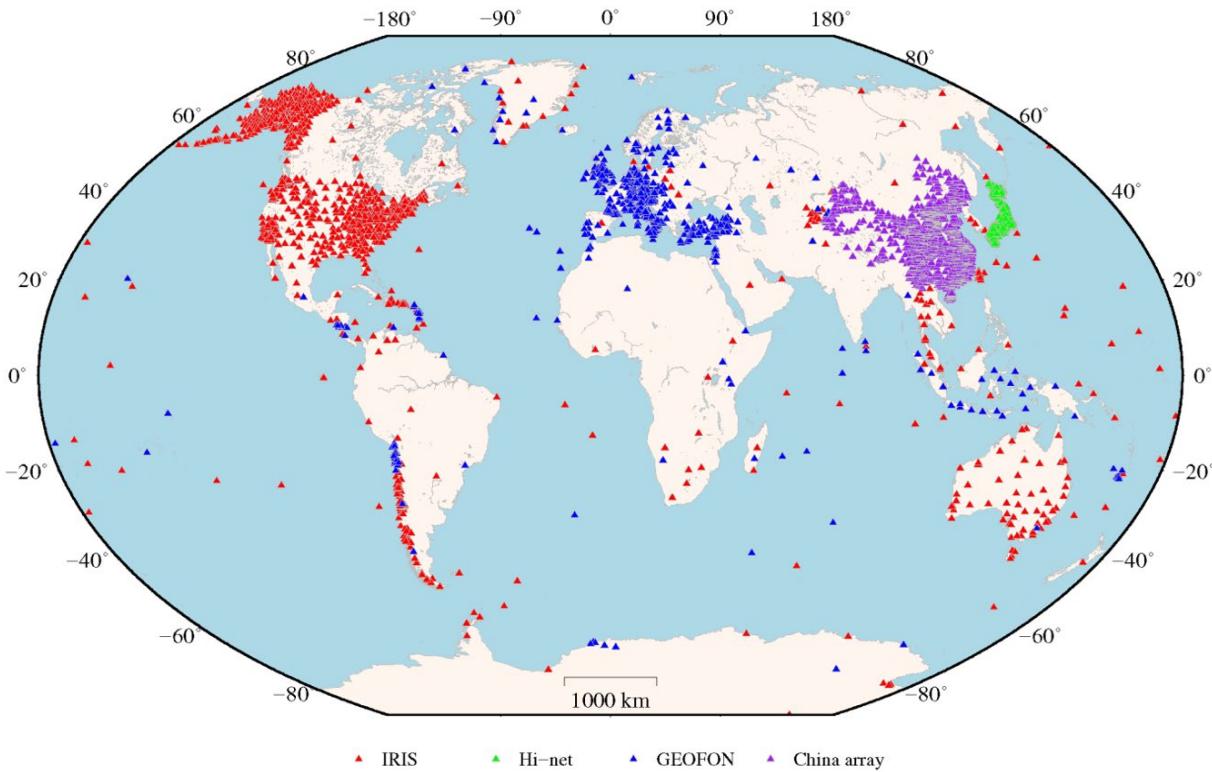
$\delta=6.61$

# Magnitude estimation for large earthquakes (2004-2021)

2004-2021/03 M $\geq$ 7 Earthquakes Worldwide (USGS)



# Magnitude estimation for large earthquakes (2004-2021)



**P Max. Disp.:**  
GSN 150+  
Global &  
Uniform

**Duration by  
BP:**  
China Array  
Japan Hi-net  
Europe Array  
US Array

# Magnitude estimation for large earthquakes (2004-2021)

$$M = \alpha \log A + \beta \log \Delta + \gamma \log t + \delta$$

Fix  $\alpha=\beta=Y=0.67$

257 large earthquakes

5 seismic arrays(GSN, China array, Japan Hi-net, USarray, EUR array)

~ 450,000 waveforms

$\delta=6.57$

$SD=0.12$

|            | $10-40^\circ$ ,         | $40-85^\circ$ , | $10-85^\circ$ |
|------------|-------------------------|-----------------|---------------|
| $\alpha$ : | <b>0.79</b> $\pm$ 0.03, | <b>0.53</b> ,   | <b>0.51</b> , |
| $\beta$ :  | <b>0.83</b> $\pm$ 0.05, | <b>0.44</b> ,   | <b>0.01</b> , |
| $\gamma$ : | <b>0.69</b> $\pm$ 0.03, | <b>1.01</b> ,   | <b>1.05</b> , |
| $\delta$ : | <b>6.47</b> $\pm$ 0.17, | <b>6.23</b> ,   | <b>7.89</b> , |
|            |                         |                 | <b>5.55</b>   |

(Hara, 2007, 2008, 2011) (Wang et al., 2017; Song et al., 2019; Yao et al., 2019)

# Magnitude estimation for large earthquakes (2004-2021)

$$\mathbf{u}^P = \frac{1}{4\pi\rho\alpha^3} \mathbf{A}^{FP} \frac{1}{r} \dot{M}_0 \left( t - \frac{r}{\alpha} \right)$$

$$M_0 = \int_0^T \dot{M}_0 = 4\pi\rho\alpha^3 r \frac{1}{\mathbf{A}^{FP}} \int_0^T u^P$$

*Mwp*  *Mdt* 

$$M_0 = \int_0^T \dot{M}_0 = 4\pi\rho\alpha^3 r \frac{1}{\mathbf{A}^{FP}} \text{Max} \left( \int_0^T |u^P| \right)$$

$$M_{wp} = \frac{1}{1.5} (\log M_0 - 9.1)$$

$$M_0 = (4\pi\rho a^3 \cdot R \cdot A) \cdot D \cdot k$$

$$M_{dt} = 0.67 * \log A + 0.67 * \log R + 0.67 * \log D + \delta$$



$$\delta=6.61$$

Rectangle

$$\delta=6.81$$

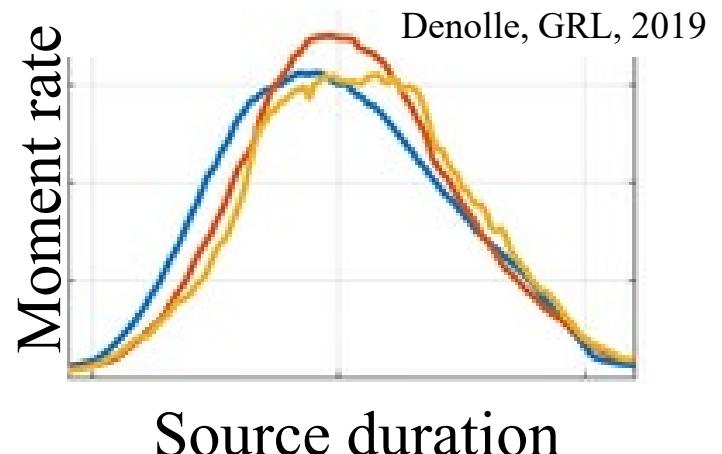
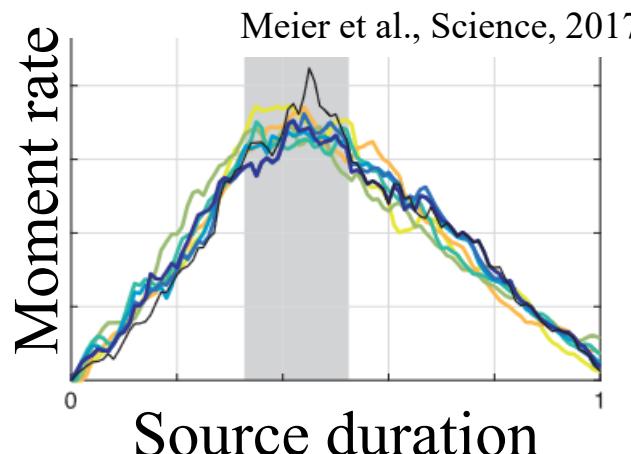
Regression Calculations:  $\delta=6.57$

# Magnitude estimation for large earthquakes (2004-2021)

$$M = \alpha \log A + \beta \log \Delta + \gamma \log t + \delta$$

Fix  $\alpha=\beta=Y=0.67$  Fitting  $\delta=6.57$

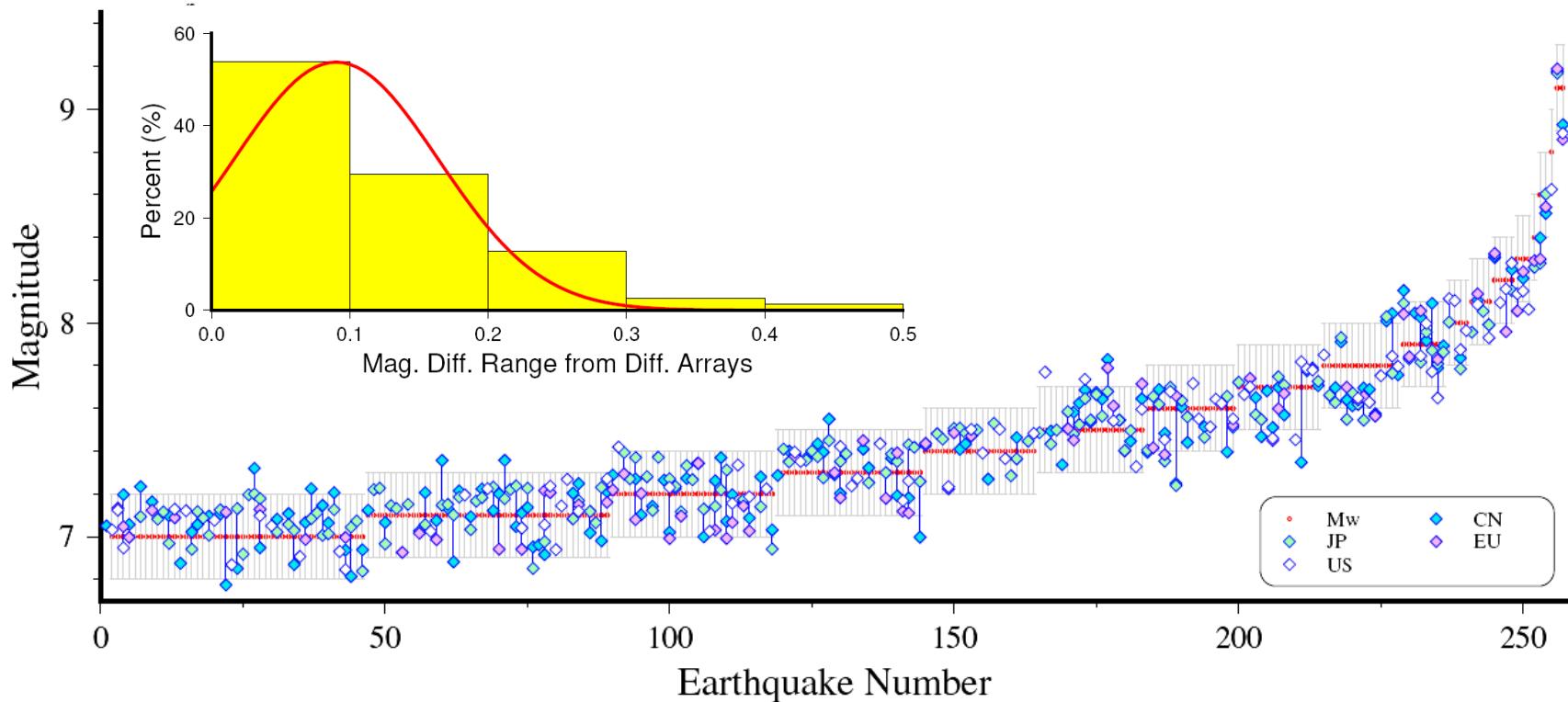
## Shape of moment rate function



- ✓ Triangle:  $\delta=6.61$
- ✓ Rectangle:  $\delta=6.81$
- ✓ Skewed normal distribution:  $6.61 < \delta < 6.81$

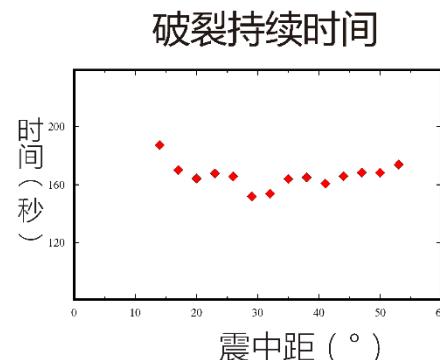
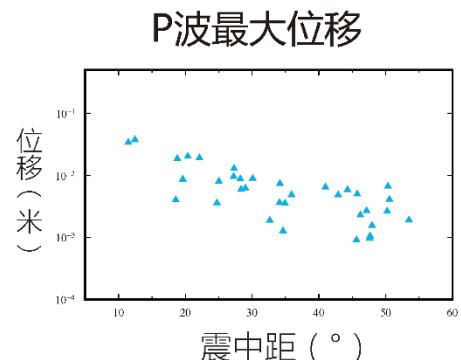
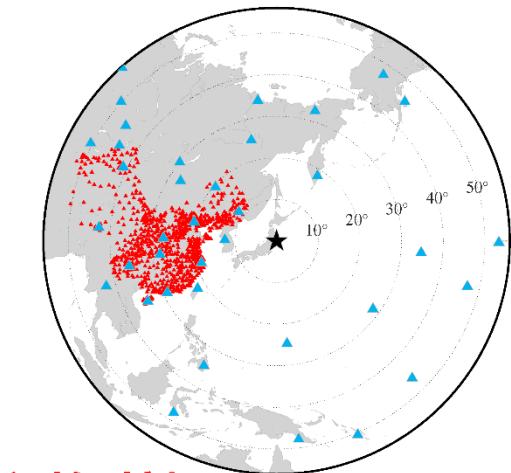
# Magnitude estimation for large earthquakes (2004-2021)

## ➤ Comparisons of Large Seismic Arrays

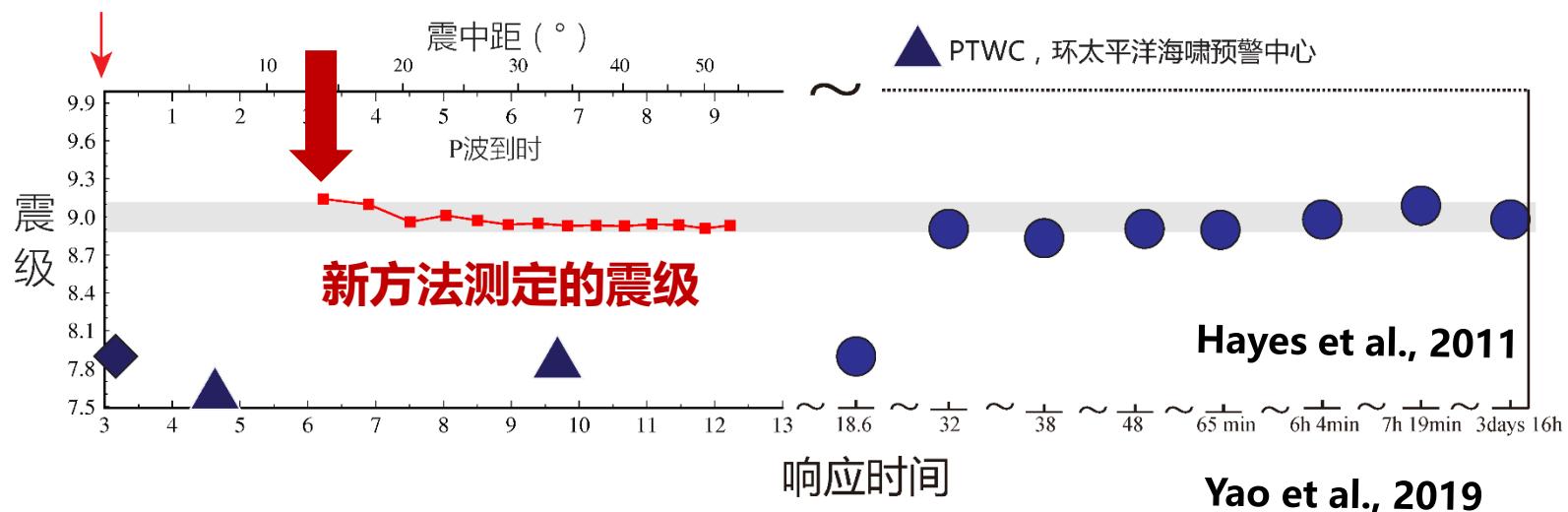


# Determining the magnitude of the M9 Tohoku earthquake

M9.1 in 6-7 min after the O.T.



初始时刻



# Determining the magnitude of the Mw 8.2 Mexico earthquake

8-15 min

USArray  
Mdt: 8.12

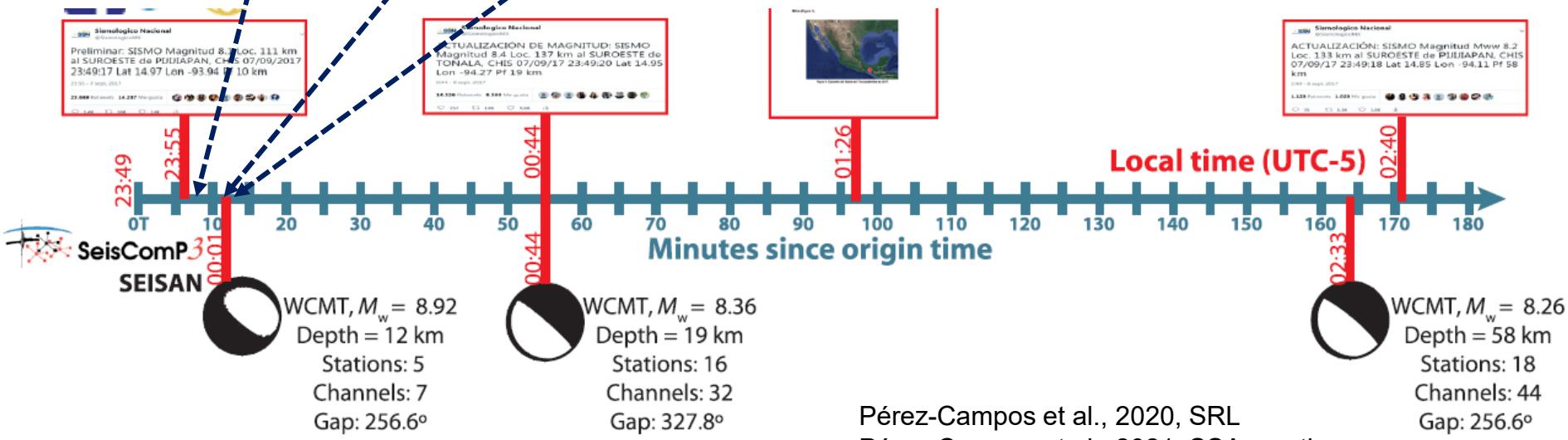
Alaska  
Mdt: 8.21

EUR  
Mdt: 8.01

~10分  
Mww 8.92

~1小时  
Mww 8.36

近2个小时后  
Mww 8.26



Pérez-Campos et al., 2020, SRL  
Pérez-Campos et al., 2021, SSA meeting.

# The 23 January 2018 Mw 7.9 Alaska earthquake

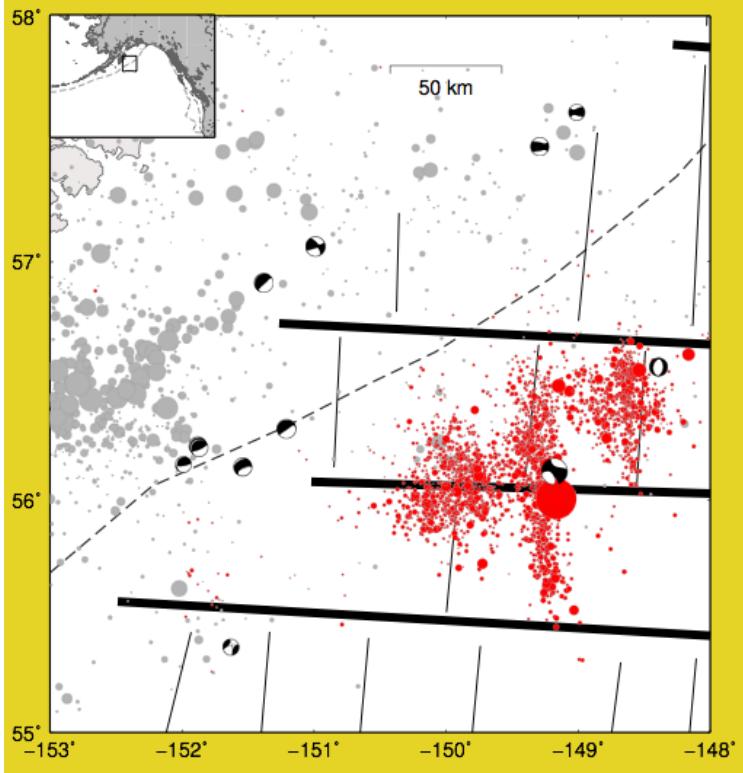
Our estimate

3-4 min,  $M_{dt}$  7.9

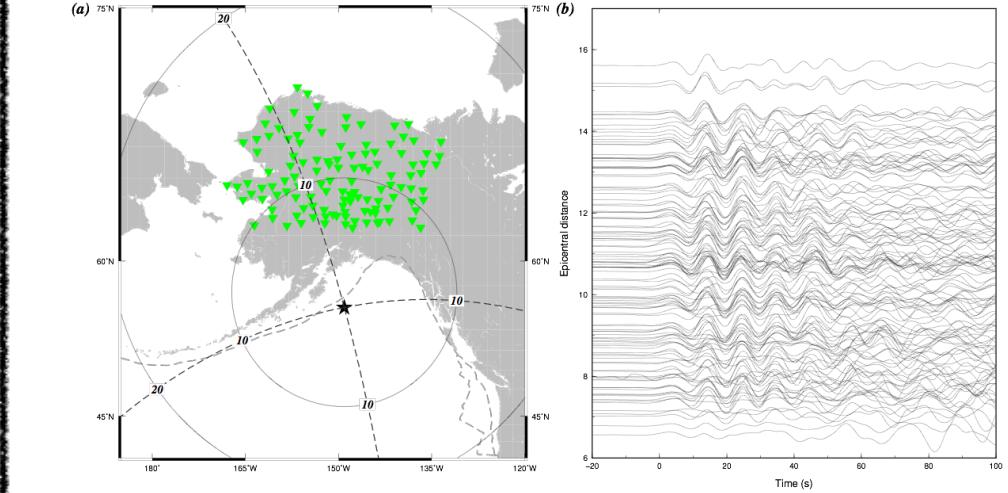
PTWC, USGS

3 min, M 8.0-8.2  
2 h, M7.9

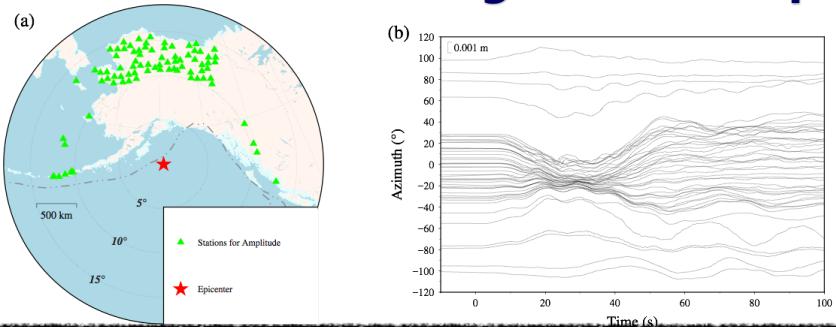
## The earthquake sequence



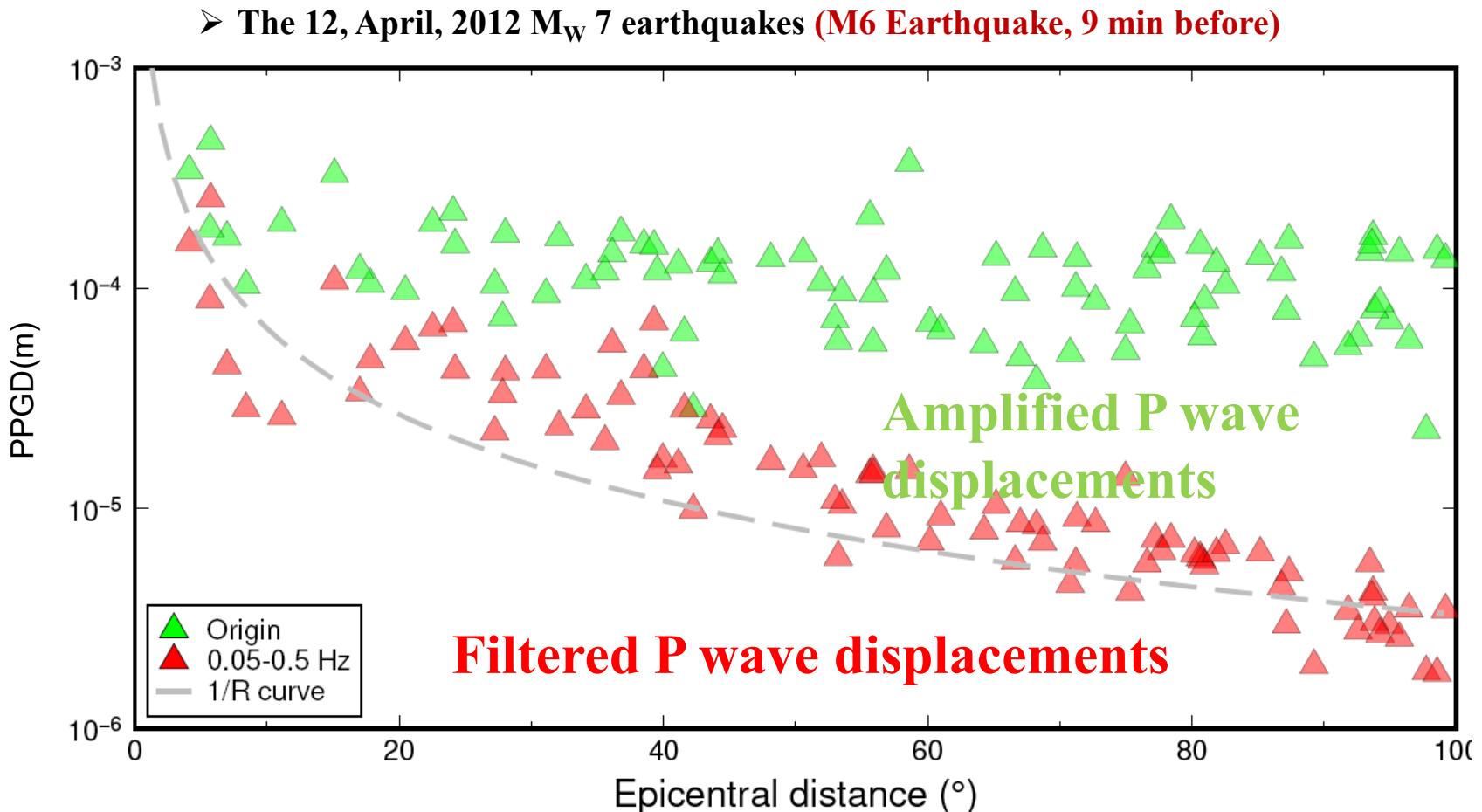
## Stations for back-projection



## Stations for calculating P-wave disp.

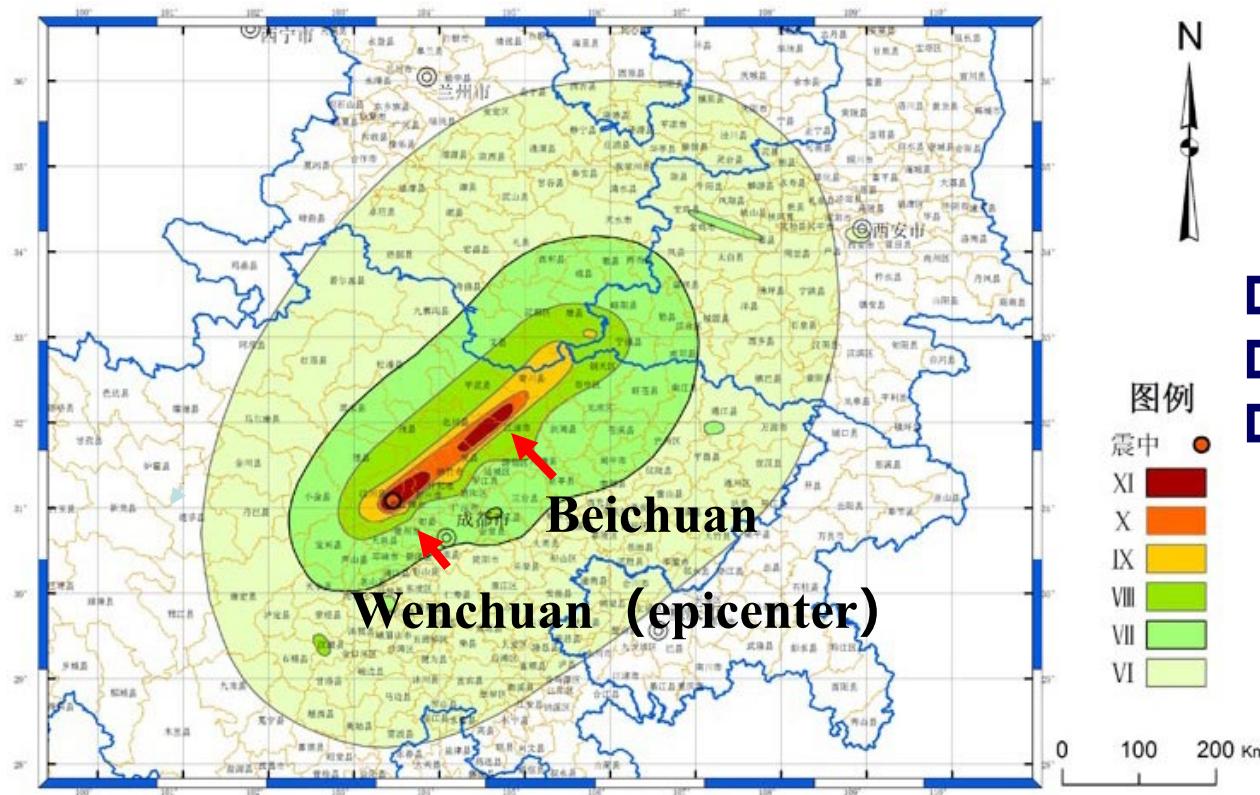


# Magnitude estimation for large earthquakes (2004-2021)



# Seismic intensity map

## Rupture fault qualifies damage areas



Seismic intensity map by field survey (CEA)

# Estimating seismic intensities

## Conventional methods

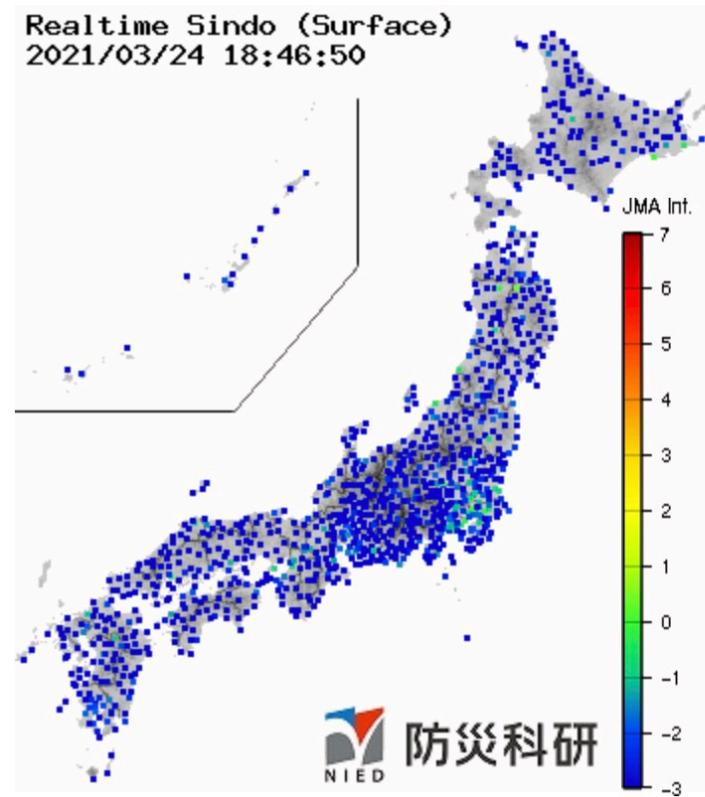
High intensity: field survey  
Low intensity: posting survey



Limited real-time observations

## Measuring ground motions

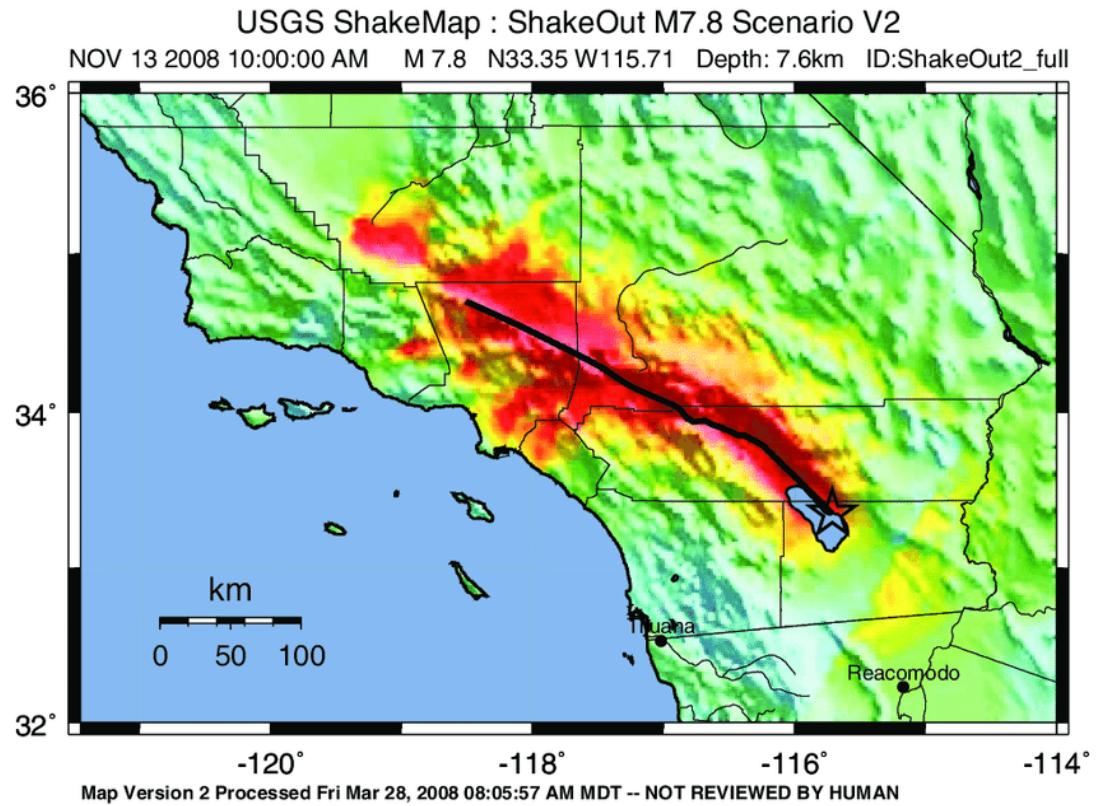
Realtime Sindo (Surface)  
2021/03/24 18:46:50



Dense real-time observations

# ShakeMap, USGS

**Sparse observation+GMPEs+DYFI**



**Unknown fault geometries will largely affect the results**

| PERCEIVED SHAKING      | Not felt | Weak    | Light   | Moderate   | Strong | Very strong | Severe         | Violent | Extreme    |
|------------------------|----------|---------|---------|------------|--------|-------------|----------------|---------|------------|
| POTENTIAL DAMAGE       | none     | none    | none    | Very light | Light  | Moderate    | Moderate/Heavy | Heavy   | Very Heavy |
| PEAK ACC.(%g)          | <.17     | .17-1.4 | 1.4-3.9 | 3.9-9.2    | 9.2-18 | 18-34       | 34-65          | 65-124  | >124       |
| PEAK VEL.(cm/s)        | <0.1     | 0.1-1.1 | 1.1-3.4 | 3.4-8.1    | 8.1-16 | 16-31       | 31-60          | 60-116  | >116       |
| INSTRUMENTAL INTENSITY | I        | II-III  | IV      | V          | VI     | VII         | VIII           | IX      | X+         |

# ShakeMap of the 2008 Mw 7.9 Wenchuan earthquake

Production time:  
(Beijing Time)

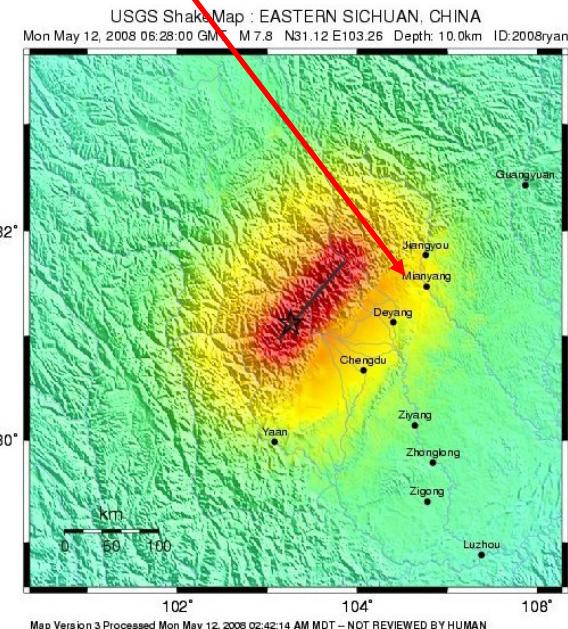
Origin Time:

2008/05/12 14:28

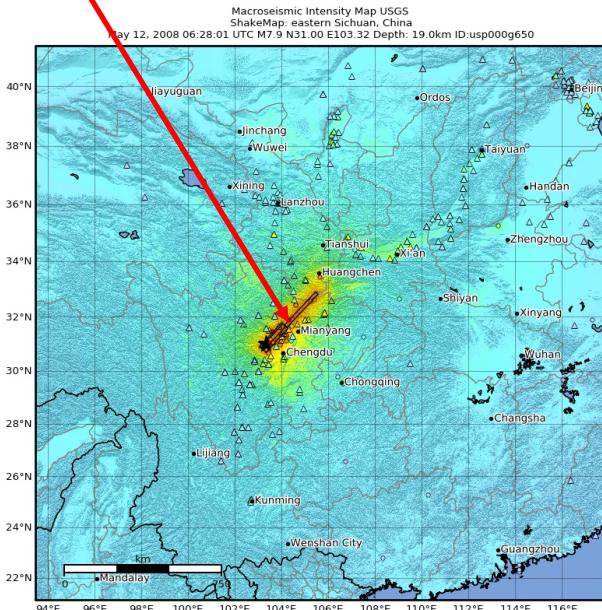
2008/05/12 17:42

2020/06/04 05:23

绵阳



绵阳



| PERCEIVED SHAKING      | Not felt | Weak    | Light   | Moderate   | Strong | Very strong | Severe         | Violent | Extreme    |
|------------------------|----------|---------|---------|------------|--------|-------------|----------------|---------|------------|
| POTENTIAL DAMAGE       | none     | none    | none    | Very light | Light  | Moderate    | Moderate/Heavy | Heavy   | Very Heavy |
| PEAK ACC.(deg)         | <0.7     | .17-1.4 | 1.4-3.9 | 3.9-9.2    | 9.2-18 | 18-34       | 34-65          | 65-124  | >124       |
| PEAK VEL.(cm/s)        | <0.1     | 0.1-1.1 | 1.1-3.4 | 3.4-8.1    | 8.1-18 | 18-37       | 37-60          | 60-118  | >118       |
| INSTRUMENTAL INTENSITY | I        | II-III  | IV      | V          | VI     | VII         | VIII           | IX      | X+         |

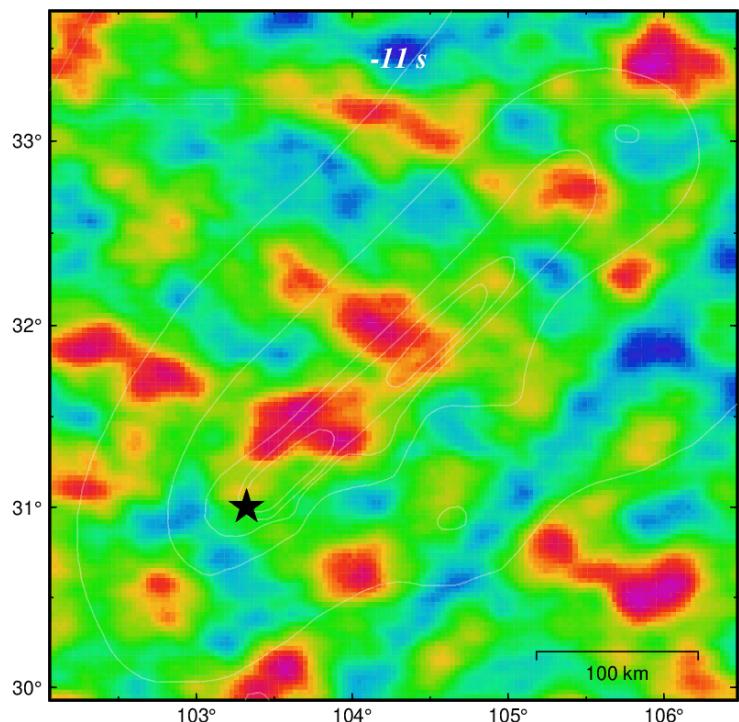
| SHAKING   | Not felt | Weak   | Light      | Moderate | Strong   | Very strong | Severe         | Violent | Extreme    |
|-----------|----------|--------|------------|----------|----------|-------------|----------------|---------|------------|
| DAMAGE    | None     | None   | Very light | Light    | Moderate | Strong      | Moderate/heavy | Heavy   | Very heavy |
| PGA(%g)   | <0.0464  | 0.297  | 2.76       | 6.2      | 11.5     | 21.5        | 40.1           | 74.7    | >139       |
| PGV(cm/s) | <0.0215  | 0.135  | 1.41       | 4.65     | 9.64     | 20          | 41.4           | 85.8    | >178       |
| INTENSITY | I        | II-III | IV         | V        | VI       | VII         | VIII           | IX      | X+         |

Version 1: Processed 2020-06-04T05:22:56Z

★ Epicenter □ Rupture

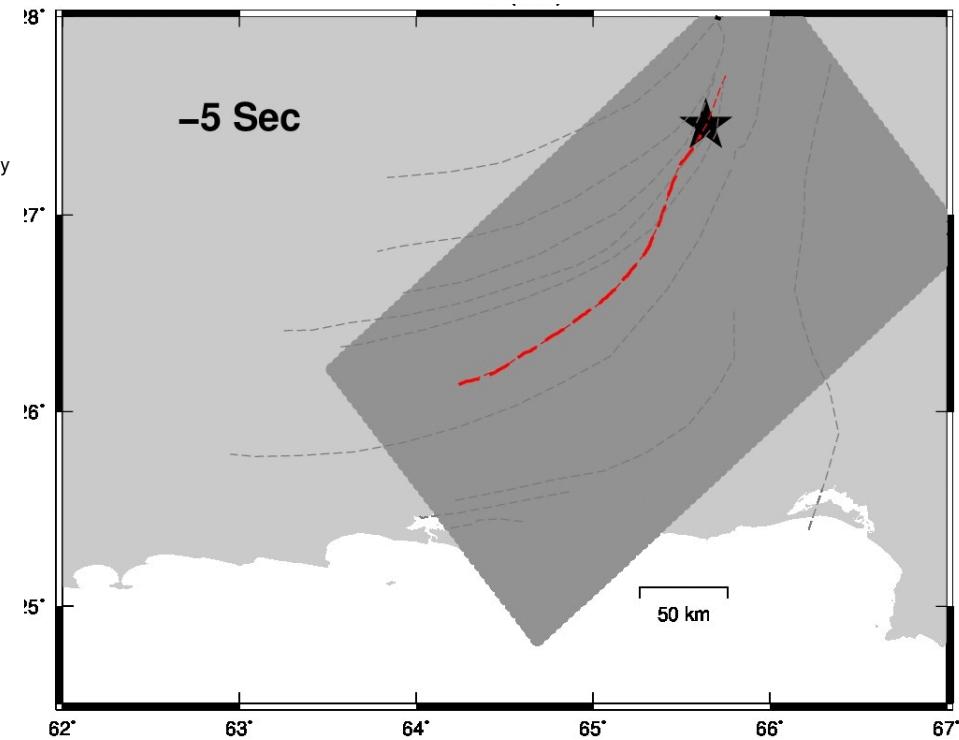
## The 12 May 2008 Mw 7.9 Wenchuan earthquake

Data: EUR, band-pass filtered 0.5-2.0 Hz



## The 24 September 2013 Mw7.7 Pakistan earthquake

Data: Hi-net, band-pass filtered 0.5-2.0 Hz

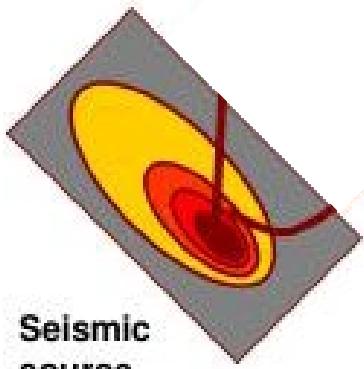


(Wang et al., 2016 )

# A novel method

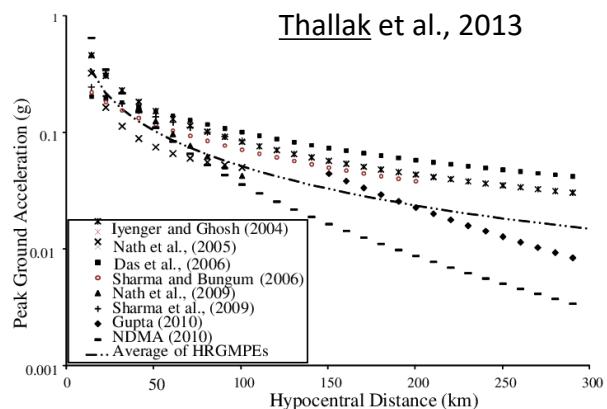
- 实时测定地震断层空间展布
- 不依赖密集强震动观测数据
- 考虑不同场地特征

Energy  
radiations

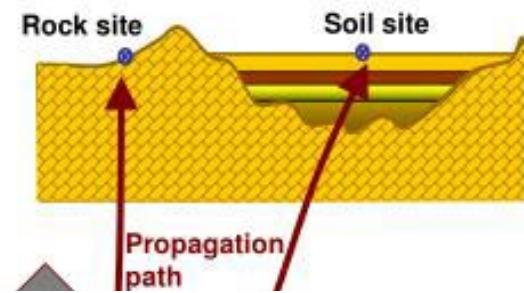


Back-projection

+ Attenuation + Site effect

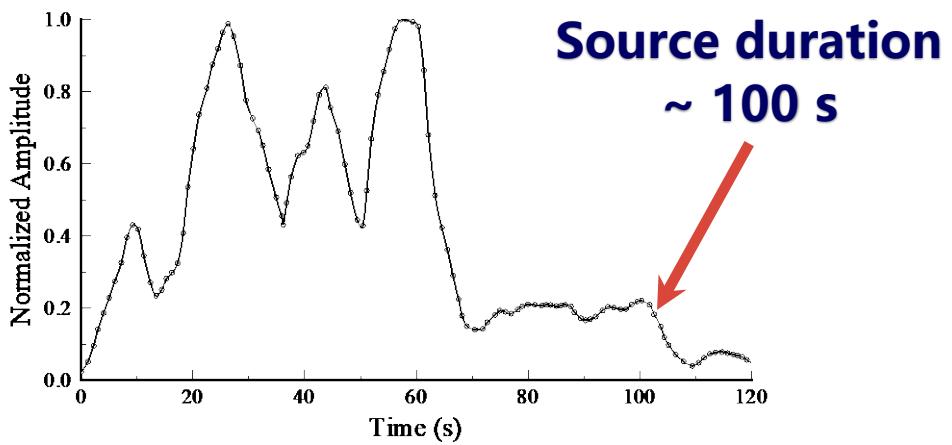
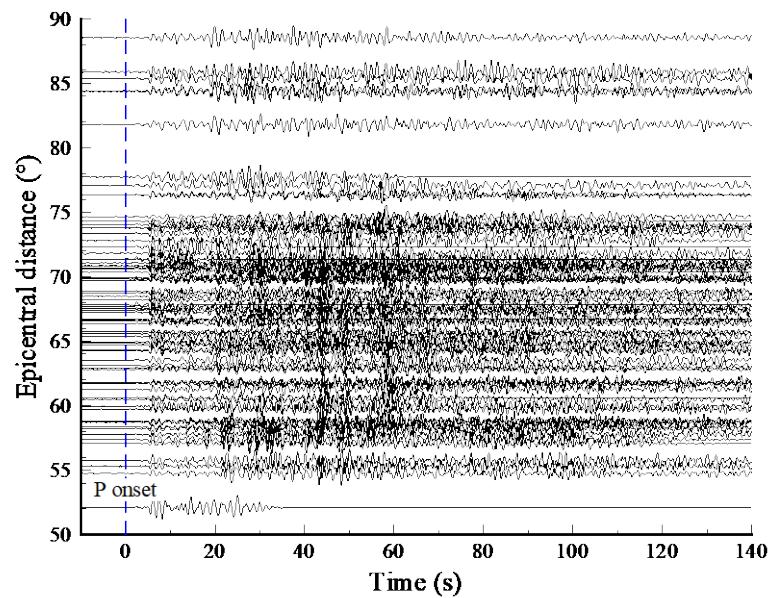
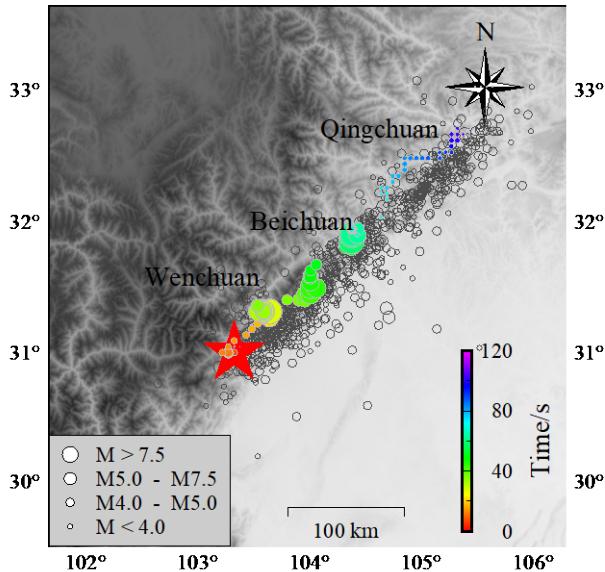
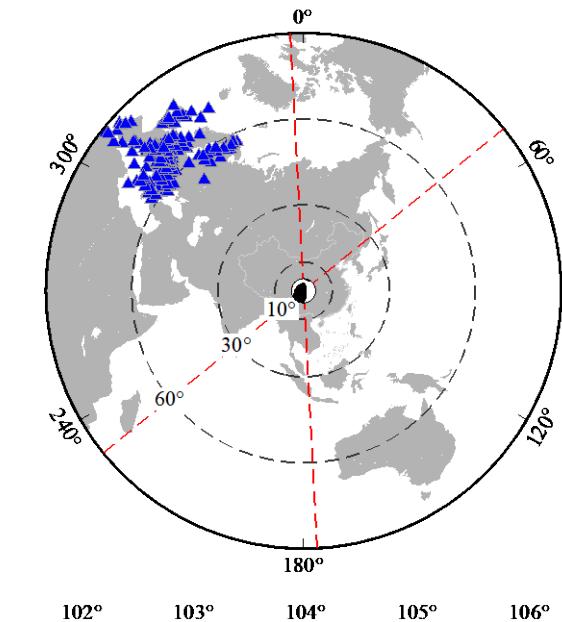


GMPEs



Site corrections  
based on  $V_{s30}$

# The 12 May 2008 Mw7.9 Wenchuan earthquake



# Seismic intensity maps

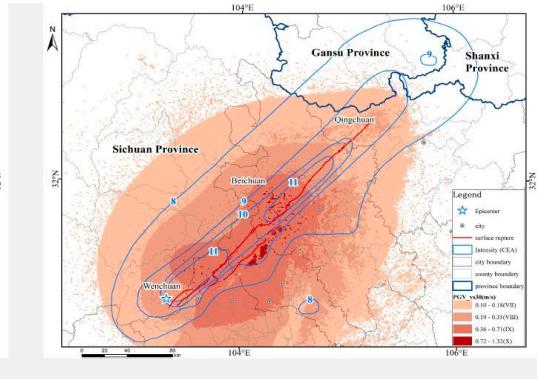
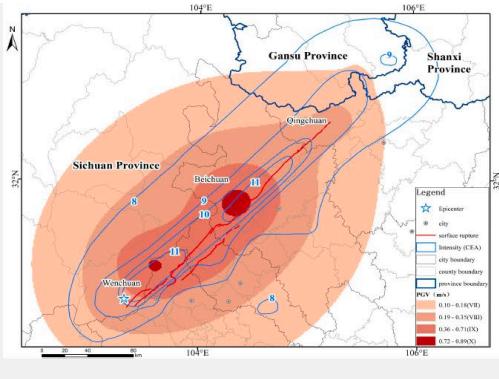
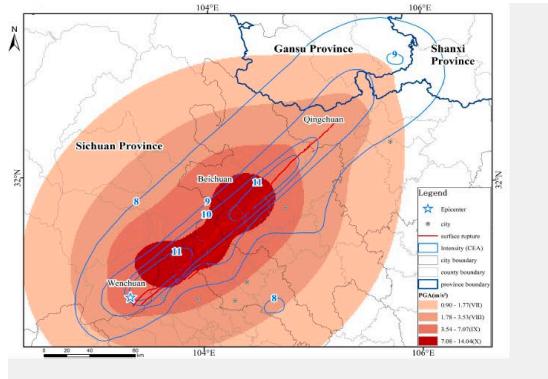
PGA

PGV

PGV site correction

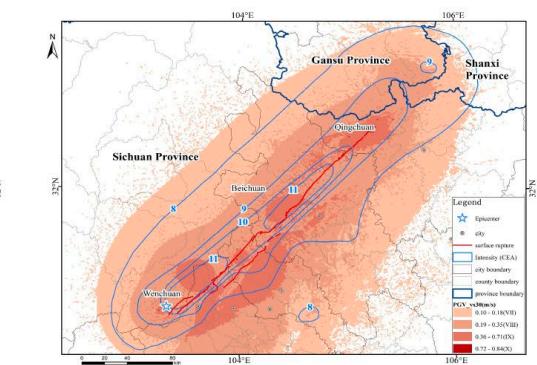
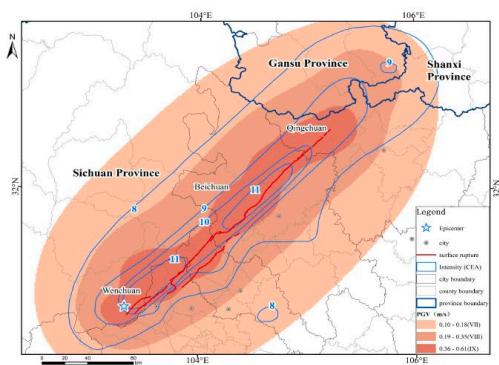
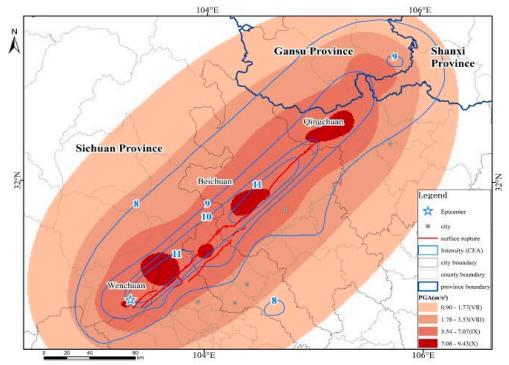
Model 1

Intensity  
and  
locations of  
subevents



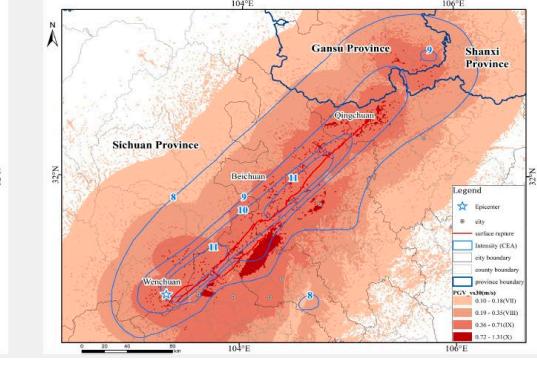
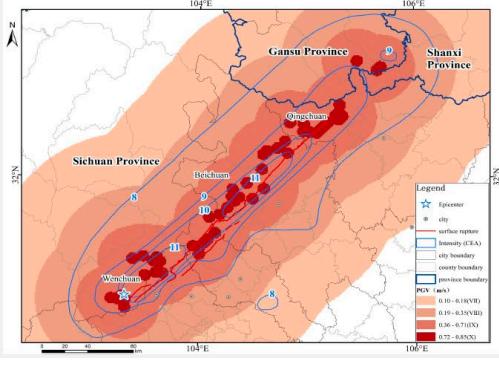
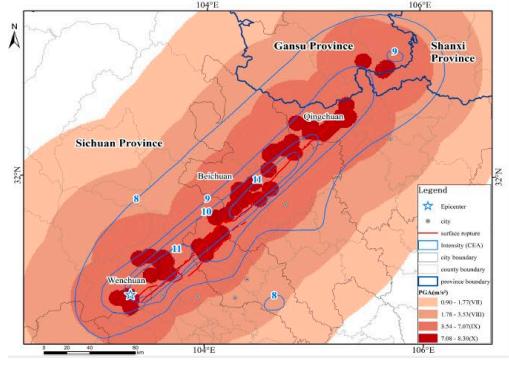
Model 2

locations of  
subevents  
Equal weight



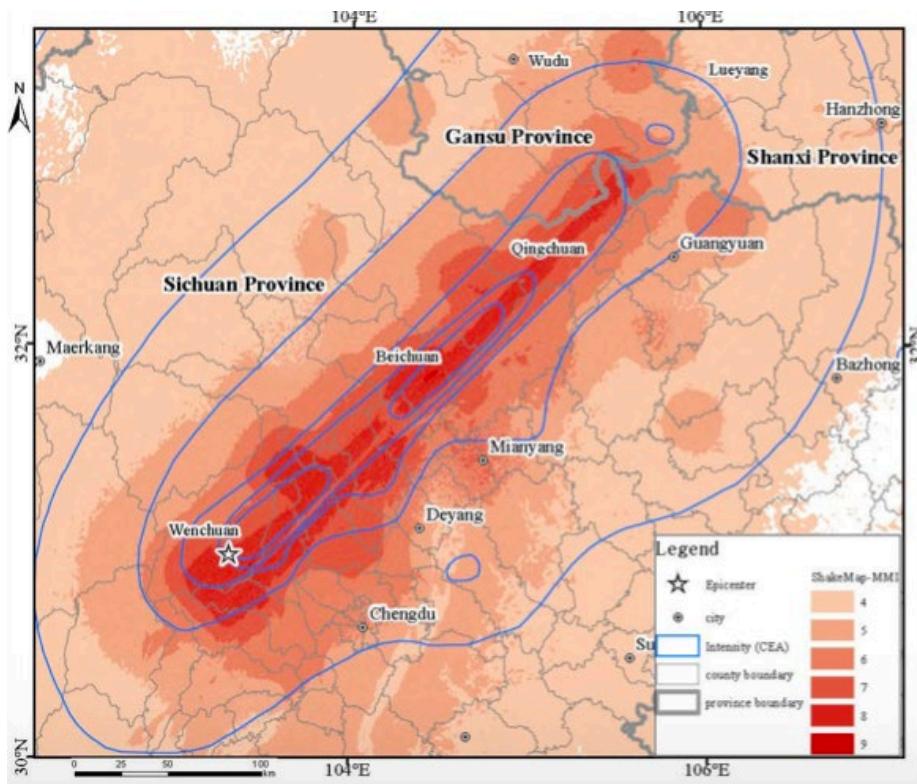
Model 3

Shortest  
distance to  
the fault  
plane



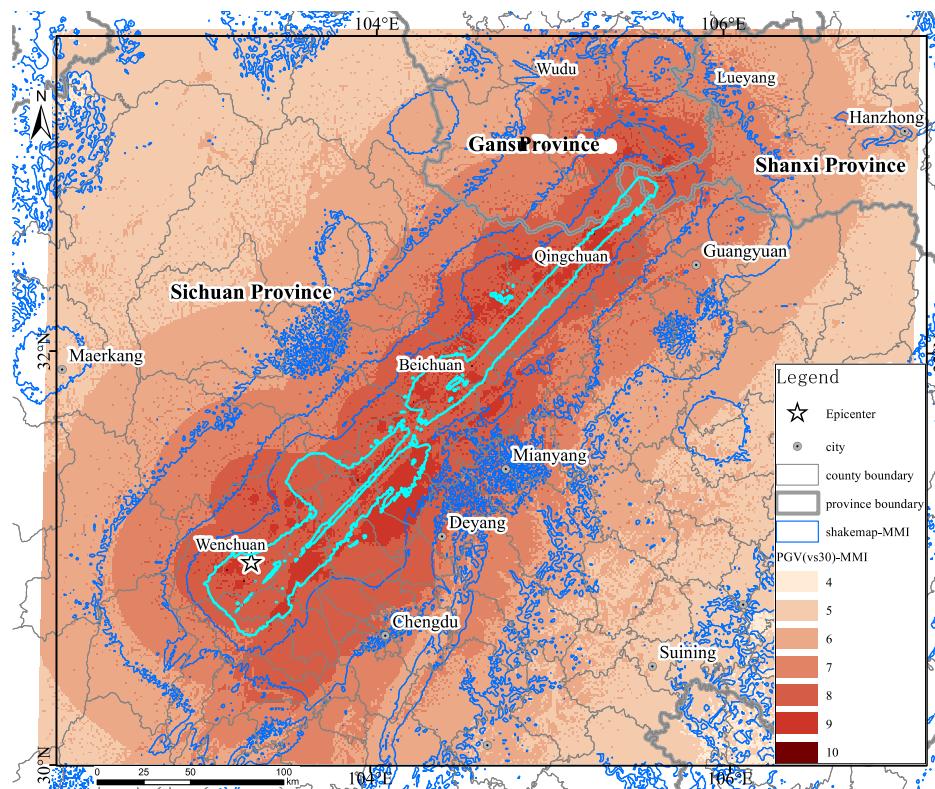
# Comparisons among seismic intensity maps of CEA, ShakeMap, and our result for the 2008 Wenchuan earthquake

## CEA & ShakeMap



蓝线：调查得到的地震烈度 (CEA)  
背景：ShakeMap结果 (2020/06)

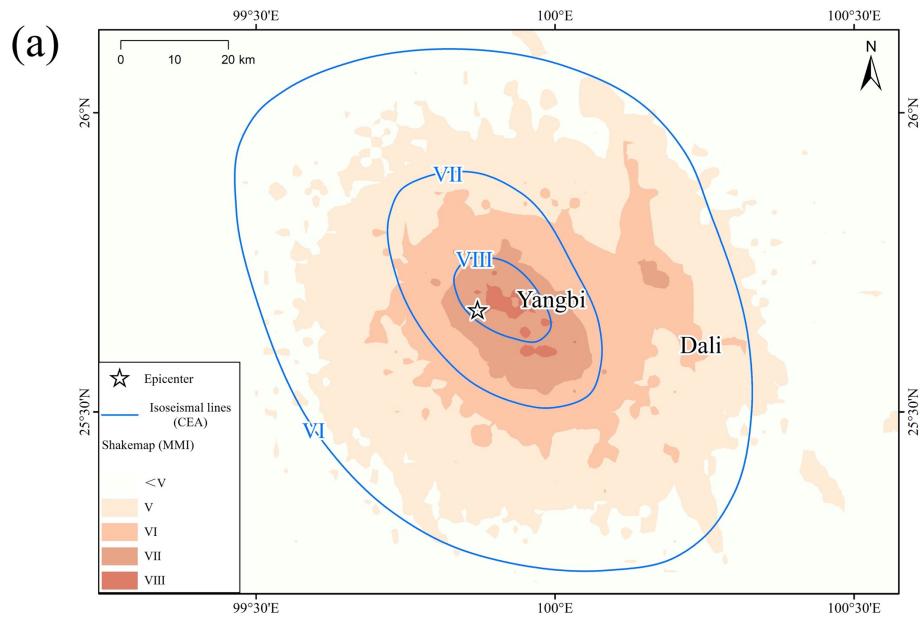
## Our result & ShakeMap



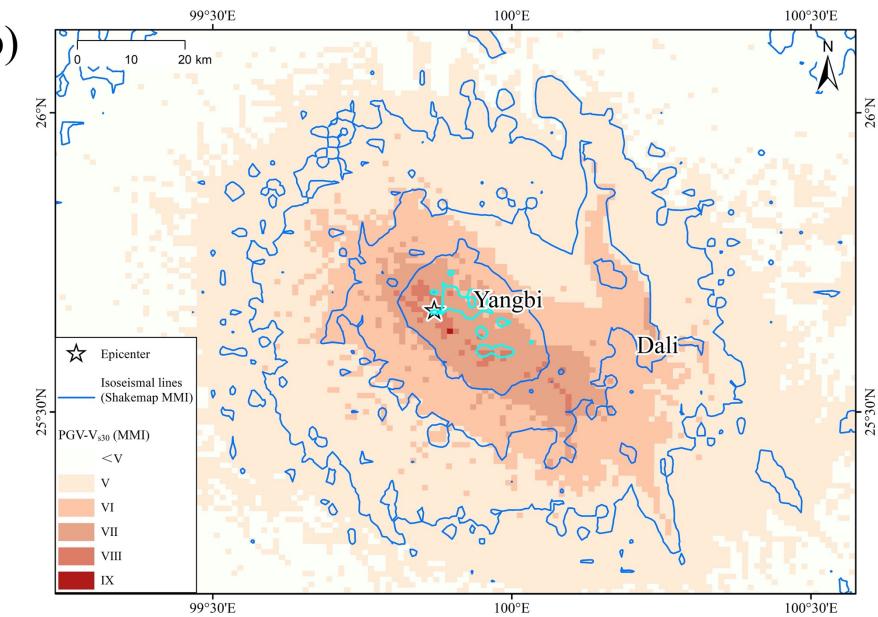
蓝线：ShakeMap结果 (2020/06)  
其中亮绿表示MMI VIII和IX度区  
背景：我们方法得到的烈度分布

# The 2021 Mw 6.1 Yangbi, Yunnan, China earthquake

**CEA&ShakeMap**



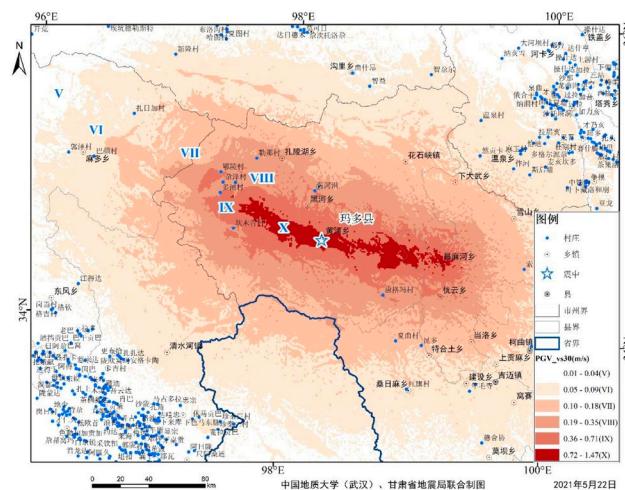
**ShakeMap&our result**



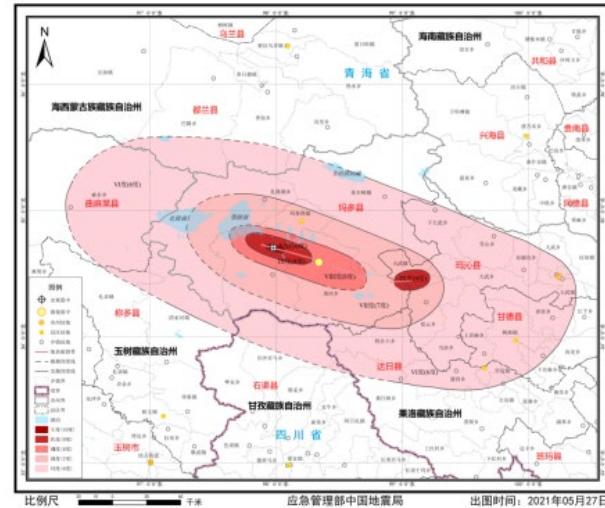
**Accurate local Vs30 is important**

# The 22 May 2021 Mw7.3 Madoi, China earthquake

4 h after the O.T.

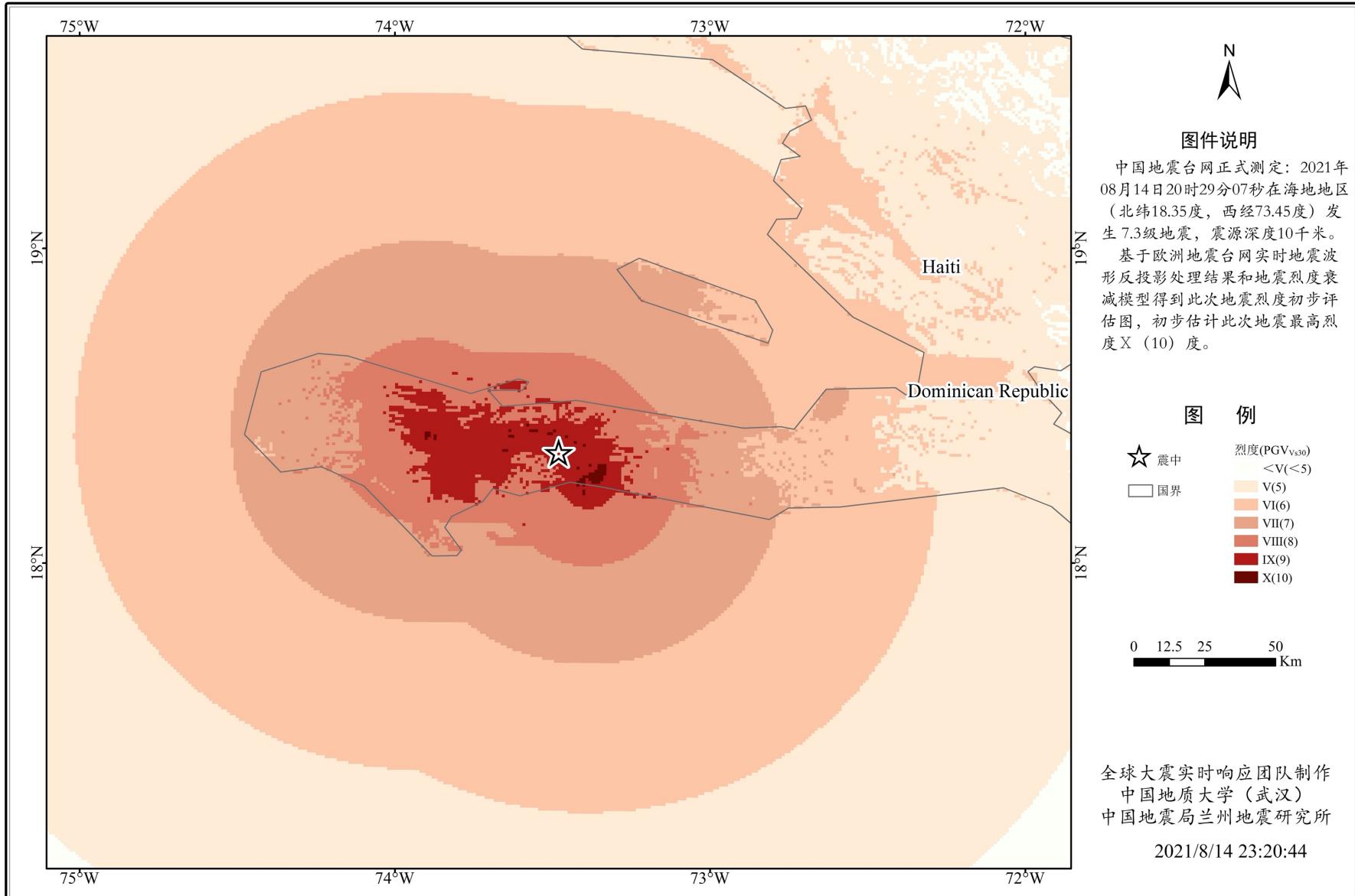


Field survey  
by the CEA



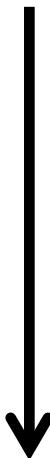
# The 14 August 2021 Mw 7.3 Haiti earthquake

## 海地M7.3级地震烈度初步评估图V1.0



# Time efficiency

**Travel time+Source duration +Data delay+ processing time**



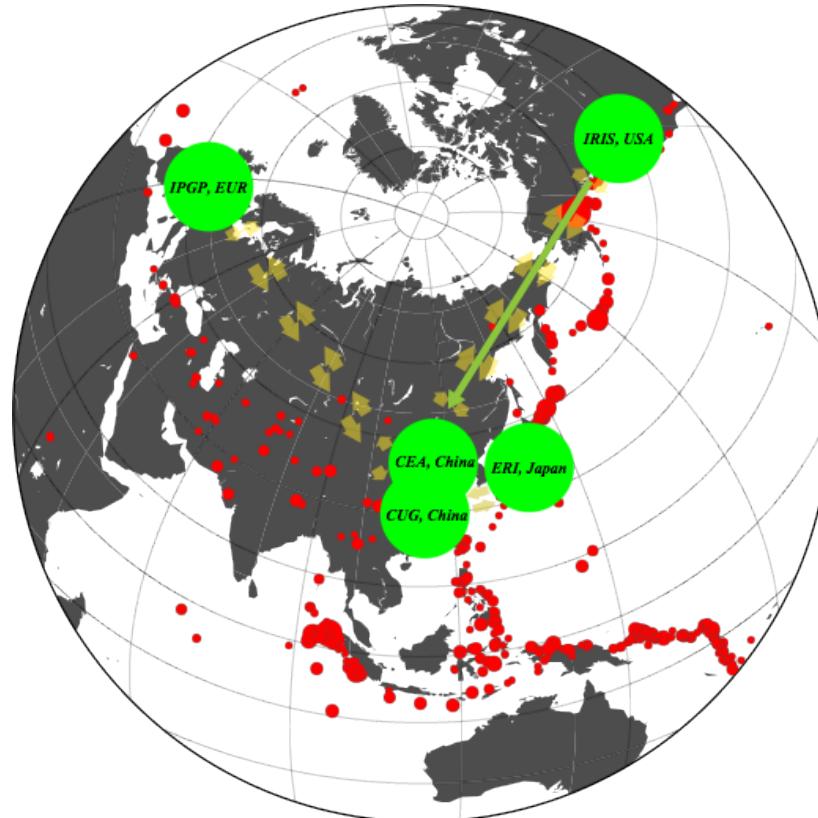
**M9 3-9 min  
M8 30s - 2 min  
M7 ~10s**

**< 1 min + < 1 min**

| Distance (Deg.)   | 10     | 30     | 50   | 90      |
|-------------------|--------|--------|------|---------|
| Distance (km)     | 1111.2 | 3335.7 | 5556 | 10000.8 |
| Travel time (min) | 2-3    | 6      | 9    | 13      |

Applying this system with three regional dense arrays that are located at Eurasia, China, Japan, and America , would help better earthquake emergency response and tsunami warning for global earthquakes.

**~10 min + Source duration**



**Thank you!**

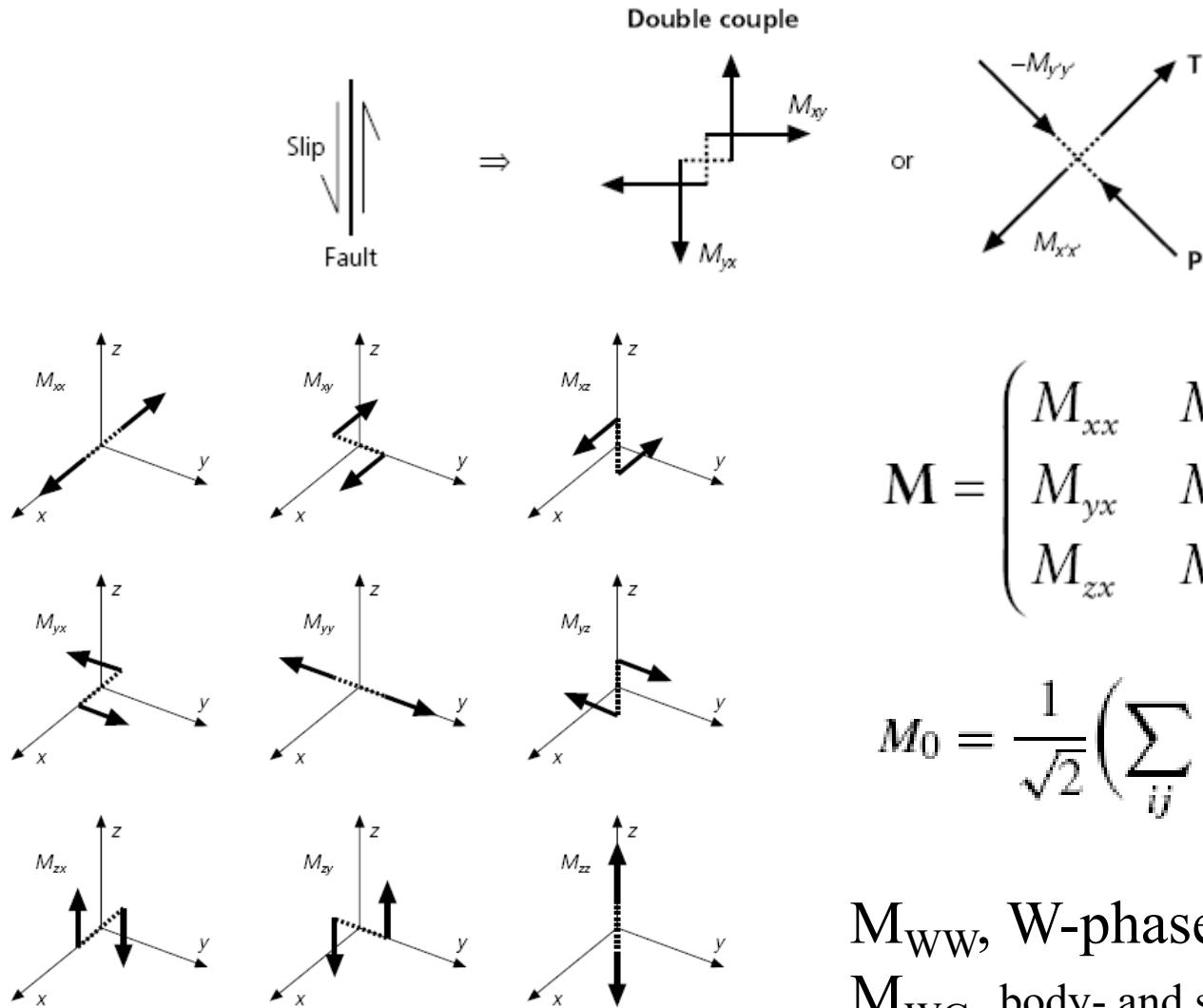
$M \geq 7.5$ , Depth  $\leq 60$  km, USGS catalog (1970-2014)







# Moment tensor inversion → Seismic moment



$$\mathbf{M} = \begin{pmatrix} M_{xx} & M_{xy} & M_{xz} \\ M_{yx} & M_{yy} & M_{yz} \\ M_{zx} & M_{zy} & M_{zz} \end{pmatrix}$$

$$M_0 = \frac{1}{\sqrt{2}} \left( \sum_{ij} M_{ij}^2 \right)^{1/2}.$$

$M_{WW}$ , W-phase, USGS, PTWC  
 $M_{WC}$ , body- and surface-waves, GCMT

# Moment Magnitude & Seismic Moment

□ **Shear module:**  $3-6 \times 10^4$  MPa for crust-upper mantle

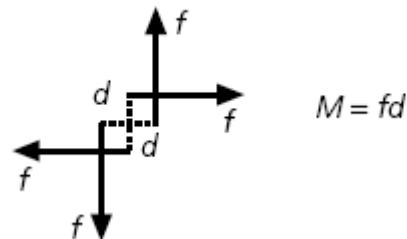
□ **Stress drop:** 2-6 MPa for large earthquakes.

$$\log E = \log M_0 + \log \frac{\Delta\sigma}{2\mu} = \log M_0 - 4.3$$

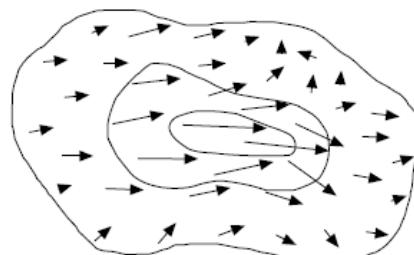
$$\lg E = 1.5M_s + 4.8 \quad \text{Gutenberg & Richter, 1956}$$

$$M_w = (\log M_0 - 4.3 - 4.8)/1.5 = (\log M_0 - 9.1)/1.5$$

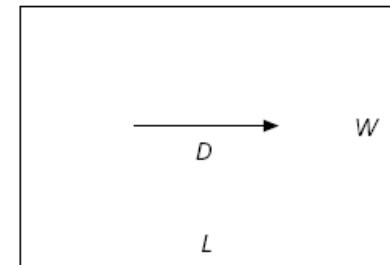
Kanamori (1977) and Hanks & Kanamori (1979)



$$M = fd$$



$$M = \int_A \mu D(A) dA$$



$$M_0 = \mu \bar{D} S$$

$$M = \mu D L W$$

